

**Teaching and Learning Practices in Secondary  
Mathematics (Teleprism)**

**Information about the Survey Methodology  
and Submitted Datasets**

**Maria Pampaka & Lawrence Wo**

**February 2015**

## CONTENTS

Methodological Overview for Surveys.....	2
The Student-Level Dataset .....	3
Variables from Part A: Identifiers and background information .....	3
Variables from Part B of Questionnaire: Feelings about Mathematics .....	5
Variables About students' Future decisions and choices .....	6
Variables About How maths is taught and learnt (Questionnaire Part D).....	8
The Mathematics Self Efficacy Items.....	9
The Constructed measures.....	9
Information received from Schools .....	11
Teacher-Class level Dataset .....	13
Teacher-Level Dataset .....	16
References .....	18
Appendices .....	19
Appendix 1 – Example Invitation Letter .....	19
Appendix 2 – The Mathematics Self Efficacy Items .....	20
Appendix 3 – MSE items by Data Point and Year Group .....	59
Appendix 4 – Example of measure construction for “Parental Involvement/Support” .....	64
Appendix 5 – SUMmary of ACCORN Types .....	67

## METHODOLOGICAL OVERVIEW FOR SURVEYS

The project was designed to capture five years of progression (Years 7-11) in slightly over one year of data collection with longitudinal surveys of students (and their teachers) at the beginning and towards the end of the first academic year (2011-2012), and at the beginning of the next academic year (2012-2013). This applies for all five secondary year groups (Year 7-11).

The proposed sampling frame, initially based on the Manchester Challenge initiative, was intended to give a sample that would provide the full spread of national demographic characteristics. Due to unforeseen circumstances with the Manchester Challenge, it was not possible to proceed with this plan, therefore an alternative sampling frame was followed. Schools were thus invited to participate using two main approaches:

1. **School contacts** of the team and other colleagues across the country (this involved schools around Manchester, Nottingham, Calderdale and Wolverhampton).
2. **Schools database** we purchased from a company. We decided to approach schools within 30 miles of various cities (to get a variety of urban/rural schools) across the country. The cities chosen were Manchester, London, Birmingham, Leeds, Bristol, Newcastle, Cambridge and Oxford (only 10 miles to avoid overlap with earlier selections)

In total, we approached over 2200 schools (an example invitation letter is shown in Appendix 1), got expressions of interest to participate from around 70 schools, and finally ended up with the **40 schools** shown in the map below:



The resulting datasets from both pupils and their teachers are provided in different sheets in the data spreadsheet, the contents of which are presented in the next sections separately.

## THE STUDENT-LEVEL DATASET

The dataset is provided in the long format, that is the data from each data point collection has been pooled together and appended together under the same variables (when applicable). A unique student id (as described below) can be used for converting the file into the wide format.

There are 18170 unique subjects (students) and 30388 records. This includes over 700 classes with 280 teachers in the first year, and over 400 classes at DP3.

The string “#NA” has been used to indicate ‘not applicable’ for:

1. Questions that did not apply to pupils of certain year groups or data points
2. Schools that did not provide background information at all or for certain fields
3. Self-efficacy items that did not get given to pupils for their particular year group

Other blanks should be treated as missing data, either due to no responses given from students, or information is not provided by the school.

Most of the variables were asked at each data point; whenever this is not the case it will be indicated explicitly in the descriptions below.

### VARIABLES FROM PART A: IDENTIFIERS AND BACKGROUND INFORMATION

These are variables with information gathered from **Part A of the student questionnaire**, complimented with some other information useful for matching data over time and across classes and schools.

Variable name	Description (with notes)	Values/Categories
<b>dp</b>	Data point for survey completion	1=October to December 2011 2=June/July 2012 3= October to December 2012
<b>unique_user_number</b>	Unique student identifier. Can be used for matching and converting the dataset to the wide format	In numeric form (N=18170)
<b>source</b>	An indicator of survey administration (i.e. the survey mode)	Hard copy Online generic – no preloaded info Online school – usernames preloaded Online school oldyear – as above but students were given different MSE items (due to admin error)
<b>school_id</b>	Unique School ID. To be used for clustering of students within schools	1 to 40
<b>year_group_se</b>	Year group version for which students completed the questionnaire	1=Year 7 2=Year 8 3=Year 9
<b>year_group</b>	Actual Year group	4=Year 10 5=Year 11 6=Year 12
<b>year_cohort</b>	The student’s cohort at the start of the survey (Oct 2011). New entries at DP3 are defined as	0=Year 7@DP3 1=Year 7 2=Year 8

	cohort 0.	3=Year 9 4=Year 10 5=Year 11
<b>class_id</b>	Unique class ID. These are only valid for use with DP1 and DP2. The IDs associated with DP3 should not be used in the same manner. They could only be used for clustering cross-sectionally.	Combination of text and numeric values, e.g. C03071 The numeric part denotes the school and the year group (i.e. School 3 and Year 7 for above).
<b>teacher1_id</b>	Teacher ID for teacher 1. The same warnings as per class ID apply here.	Combination of text and numeric values, e.g. T0307 The numeric part denotes the school id.
<b>teacher2_id</b>	Teacher ID for teacher 2. The same warnings as per class ID apply here.	As above
<b>dp_teacher_class1</b>	A variable that combines the information for dp, teacher1_id and class_id. Useful for matching with teacher-class level data.	Combination of text and numeric values combining together information on DP, teacher and class.
<b>dp_teacher_class2</b>	A variable that combines the information for dp, teacher2_id and class_id. (as above)	As above
<b>gender</b>	The gender of student.	1 = Male 2 = Female
<b>favourite_subject</b>	Which is your favourite subject in school?	Open responses
<b>least_favourite_subject</b>	Which is your least favourite subject in school?	Open responses
<b>maths_choice</b>	A new variable developed considering the combination of answers in the two previous questions.	0=maths listed as least favourite, 1=not mentioned, 2=maths mentioned as favourite
<b>ability_maths</b>	How do you rate your ability in the following subjects: Maths	1=poor, 2=average, 3=good, 4=excellent
<b>ability_english</b>	How do you rate your ability in the following subjects: English	1=poor, 2=average, 3=good, 4=excellent
<b>ability_science</b>	How do you rate your ability in the following subjects: Science	1=poor, 2=average, 3=good, 4=excellent
The following three variables were only asked at DP2 and DP3, with these questions: How has your ability in these subjects changed since the beginning of the year? (DP2) How has your ability in these subjects changed since last year? (DP3)		
<b>ability_change_maths</b>	Maths	1= worse now
<b>ability_change_english</b>	English	2=same
<b>ability_change_science</b>	Science	3=better now
The next variables give responses to: How often do your parents do the following?		
<b>parents1</b>	Check whether you have done your homework	1 = Never
<b>parents2</b>	Help you with your homework	2 = Rarely
<b>parents3</b>	Praise or reward you for good grades	3 = Sometimes
<b>parents4</b>	Reduce your rewards because of low grades	4 = Often
<b>parents5</b>	Find you a tutor to help you with your homework	5= All the time

## VARIABLES FROM PART B OF QUESTIONNAIRE: FEELINGS ABOUT MATHEMATICS

The three variables listed in the table below were only asked with the new cohort (0) year 7 students at DP3.

Variable Name	Question in Questionnaire	Codes
<b>Biggest_Change</b>	What has been the biggest change for you, moving from primary to secondary school?	Open response
<b>Teaching_Change</b>	Has the way you been taught by teachers changed? If so, how?	Open response
<b>Maths_Change</b>	How is mathematics different from primary school?	Open response

The next variables include information gathered from Part B of the student questionnaire (from all students). These items were also used for the construction of the measures of 'maths disposition' and 'maths identity'.

Variable name	Description (with questions)	Values/Codes
<b>How much do you agree or disagree with the following statements:</b>		
<b>statement1</b>	Mathematics is important to me	1=SD 2=D 3=Unsure 4=A 5=SA
<b>statement2</b>	Most people can learn to be good at maths.	
<b>statement3</b>	My parents/carers like maths.	
<b>statement4</b>	Maths is one of the most interesting school subjects.	
<b>statement5</b>	Learning maths is enjoyable for me.	
<b>statement6</b>	I have a mathematical mind.	
<b>statement7</b>	I can get good results in maths.	
<b>statement8</b>	I am interested in learning new things in maths.	
<b>statement9</b>	In maths you get rewards for your effort.	
<b>statement10</b>	Being good at maths is something you are born with.	
<b>statement11</b>	I can learn maths even if it is hard.	
<b>statement12</b>	I like using maths I am familiar with rather than new maths topics.	
<b>statement13</b>	I am more worried about maths than any other subject.	
<b>statement14</b>	I often need help with maths.	
<b>statement15</b>	Compared to my classmates, I am good at maths.	
<b>statement16</b>	My parents/carers enjoy solving mathematical problems.	
<b>statement17</b>	I never want to take another mathematics course.	
<b>statement18</b>	I would prefer my future studies to include a lot of maths.	
<b>statement19</b>	I would look forward to studying more mathematics after school.	
<b>statement20</b>	I would like to be a mathematician.	
<b>statement21</b>	Maths is important for my future (after school)	

The next two questions and resulting variables are only available for Years 10 and 11.

Y10 & Y11 ONLY		
<b>more_maths</b>	Are you planning to study any more mathematics courses or units after this GCSE course? (e.g. AS, A2)	1=Yes 2=No 3=I don't know
<b>more_maths_details</b>	If yes, please give details. If no, why not?	Open response

## VARIABLES ABOUT STUDENTS' FUTURE DECISIONS AND CHOICES

The following variables resulted from Part C of the questionnaire about student's plans for the future and major influences on their decisions and choices.

Variable name	Description (or questions asked)	Values/Categories
<b>prefer_first_choice</b>	Which of the following options would you prefer to do when you finish Year 11 A. Continue studying at this school B. Study full-time at a college C. Study part-time at a college while working D. Take an apprenticeship (a training course in a practical subject, e.g. plumbing, hairdresser, etc)	A to H
<b>prefer_second_choice</b>	E. Work in the family business F. Work in a full-time job G. Work in a part-time job H. Other	A to H
<b>prefer_other</b>	Information regarding 'other' option.	Open
<b>prefer_confidence</b>	How confident are you that you will be able to get your first choice	1=Not at all confident 2=Somewhat confident 3=Very confident

The following two questions were only asked from students in Years 10 and 11.

Variable name	Description (or questions asked)	Values
<b>continue_education</b>	Do you plan to continue your education after Year 11?	1=Yes 2=No 3=I don't know
	If you choose 'Yes', please choose one of the following options:	
<b>continue_education_details</b>	I will continue my education right after Year 11 (GCSEs) in secondary school I will continue my education after staying out of school for one year (or more) I will continue my education, but I don't know when	1= ticked first 2= ticked second 3= ticked third

The following are potential factors that might stop them from continuing their education:

Variable name	Description (or questions asked)	Values/Categories	Notes
	Which of these might stop you from continuing your education after Year 11		
<b>stop1</b>	Low GCSE grades	1 or empty	if ticked the corresponding column is marked with the equivalent number of item
<b>stop2</b>	Parents	2 or empty	
<b>stop3</b>	Friends	3 or empty	
<b>stop4</b>	Other relatives	4 or empty	
<b>stop5</b>	Leaving friends and family	5 or empty	
<b>stop6</b>	Uninterested in studying	6 or empty	
<b>stop7</b>	Care responsibilities	7 or empty	
<b>stop8</b>	Don't know what to do	8 or empty	
<b>stop9</b>	Full-time job	9 or empty	
<b>stop10</b>	Don't like school	10 or empty	
<b>stop11</b>	School not important	11 or empty	
<b>stop12</b>	Not enough money	12 or empty	
<b>stop13</b>	None of the above	13 or empty	

The following variables are about potential influences regarding their decisions, as well as whether other members of their family have been to university.

Variable name	Description (or questions asked)	Values/Categories
	Who will influence or inspire your decisions about what you want to do after Year 11	
<b>influence1</b>	My friends	1=YES 2=Maybe 3=NO
<b>influence2</b>	My parents	
<b>influence3</b>	Teachers	
<b>influence4</b>	My brothers or sisters	
<b>influence5</b>	My cousins	
<b>influence6</b>	Other relatives (aunts, uncles, grandparents)	
<b>influence7</b>	Counsellors at school	
<b>influence8</b>	Other	
<b>influence_details</b>	Information regarding 'other' option.	OPEN
<b>job_description</b>	What job would you like to do in the future?	OPEN
<b>job_reason</b>	Why?	OPEN
<b>go_uni</b>	Do you plan to go to university?	1=Yes 2=No 3=I don't know
<b>uni_course</b>	If you plan to go to university, what subject would you most like to study?	OPEN
	Please also tell us if you know of any people who have been to university by ticking the appropriate box in the following table	
<b>been_uni1</b>	My parents/carers	1=YES 2=NO 3=At uni now 4=I don't know
<b>been_uni2</b>	My brothers or sisters	
<b>been_uni3</b>	My friends	
<b>been_uni4</b>	My cousins	
<b>been_uni5</b>	Other relatives (aunts, uncles, grandparents)	
<b>been_uni6</b>	Other	
<b>been_uni_details</b>	Information regarding 'other' option.	OPEN



## VARIABLES ABOUT HOW MATHS IS TAUGHT AND LEARNT (QUESTIONNAIRE PART D)

These variables are from Part D of the questionnaire and aim to capture students' perceptions of the way maths was taught and learnt. Variables "lessons1" to "lessons26" also served as the items in Rasch Modelling of what we called 'perceptions of transmissionist teaching' and 'perceptions of teaching variation' (as described below).

Variable name	Description (or questions asked)	Values/Categories
<b>lessons1</b>	The teacher asks us questions.	1= Never 2=Rarely 3=Sometimes 4=Always
<b>lessons2</b>	The teacher asks us to explain how we get our answers.	
<b>lessons3</b>	The teacher starts new topics with problems about the world.	
<b>lessons4</b>	The teacher tells us to work more quickly.	
<b>lessons5</b>	The teacher uses the computer to teach some topics.	
<b>lessons6</b>	The teacher gives us problems to investigate.	
<b>lessons7</b>	The teacher expects us to remember important ideas learnt in the past.	
<b>lessons8</b>	The teacher tells us which questions/activities to do.	
<b>lessons9</b>	The teacher asks us what we already know about a lesson topic.	
<b>lessons10</b>	The teacher tells us what value the lesson topic has for future use.	
<b>lessons11</b>	We work together in groups on projects.	
<b>lessons12</b>	We listen to the teacher talk about the topic.	
<b>lessons13</b>	We copy the teacher's notes from the board.	
<b>lessons14</b>	We talk with other students about how to solve problems.	
<b>lessons15</b>	We ask other students to explain their ideas.	
<b>lessons16</b>	We do projects (assignments) that include other school subjects.	
<b>lessons17</b>	We work through exercises from the textbook.	
<b>lessons18</b>	We learn how mathematics has changed over time.	
<b>lessons19</b>	What we learn is related with our out-of-school life.	
<b>lessons20</b>	We learn that mathematics is about inventing rules.	
<b>lessons21</b>	We get assignments to research topics on our own.	
<b>lessons22</b>	We use calculators.	
<b>lessons23</b>	We use computers.	
<b>lessons24</b>	We use other things like newspapers, magazines, or video.	
<b>lessons25</b>	We discuss ideas with the whole classroom.	
<b>lessons26</b>	We explain our work to the whole class.	
<b>lesson_difficulty</b>	Most of the time my maths lessons feel:	1=Too easy 2=About right 3=Too hard
	If you use computers or the calculators for your maths lessons, please tell us what are you using them for:	
<b>computers</b>	We use computers for...	OPEN
<b>calculators</b>	We use calculators for...	OPEN

## THE MATHEMATICS SELF EFFICACY ITEMS

This section lists all items presented in Section E of the student questionnaire, matched across data points and year group cohorts. A total of 79 items were used all followed by these instructions.

### Part E- How confident are you with different topics in mathematics?

In this section, we are asking you to say how confident you would be at using mathematics to solve different problems. **We don't ask you to actually solve the problems.**

Imagine that you have been given the following questions to do. You would be able to use your notes, textbooks, calculator, and so on when necessary. Please tell us how confident you are that you would be able to solve each problem, **without actually doing the problem.**

**How confident are you that you are able to solve problems of the kind given in each case?**

**Please circle one response for each task.**

The whole list of items' pictures is presented in Appendix 2, in the order they appear in the dataset. All items were coded with the following values:

- 1=Not confident at all
- 2=Not very confident
- 3=Fairly confident
- 4=Very confident

Appendix 3 lists the items given to each year group at each data point.

## THE CONSTRUCTED MEASURES

The next group of 'variables' given in our datasets goes beyond row data and presents the results of the second step of our analytical approach; more details about our comprehensive analytical approach which involves instrument construction, measure validation and analysis see our earlier work (Pampaka, Williams, & Hutchenson, 2012; Pampaka, Williams, Hutchenson, et al., 2012). Therefore we present the results of our validation of certain constructs based on students' responses to previously stated items. This is based on the assumption that there is an underlying construct (or idea/concept) behind the groups of items in the questionnaires, which were brought together after studying previous research literature and looking at other researchers' instruments. Following this with our questionnaires we intended to measure the following ideas/constructs (with the items related to each one presented in the next sections):

- Parental support/involvement
- Attitudes to mathematics
- Mathematics Self-efficacy
- Perceptions (of transmissionist) teaching

Given the students' responses to the relevant questions we then attempt to validate these aforementioned constructs: in other words to check whether they exist as "measures" (or scales), and if not whether there are other dimensions relevant and useful. So, our validation process refers to the accumulation of evidence to support validity arguments regarding the students' reported measures (Messick, 1988, 1989). We employed a psychometric analysis for this purpose, conducted within the Rasch measurement framework, and following relevant proposed guidelines (Wolfe & Smith Jr., 2007a, 2007b). The Rasch rating scale model (using the Winsteps software) is considered the most appropriate for the scaling involved in this project (i.e. a common Likert type scale). Our decisions about the validity of the measures are based on different statistical indices, such as item fit statistics, category statistics, differential item functioning and person-item maps (Andrich, 1999; Bond & Fox, 2001; Thissen, Steinberg, & Wainer, 1993; Wright & Masters, 1982; Wright & Mok, 2000). An example of how these statistical indices are used in order to validate the measure of students' 'perceived parental support/involvement' are shown in Appendix 4, while elsewhere (Pampaka & Wo, 2014) we present details about the construction of maths disposition and 'identity' measures. More details about other measures along with relevant publications will be uploaded in our website ([www.teleprism.com](http://www.teleprism.com)).

The next table summarises our constructed measures with reference to the items used, and some broad working definition of the 'construct' developed:

Measure Name	Items used	'Construct' description
<b>parental support</b>	Parents1 to Parents5	Students' perceived parental involvement/support
<b>maths disposition</b>	Statement1, 4, 5, 8, 17, 18, 19, 20 and 21	Measure related to expressions of behavioural intention for future engagement with mathematics (the higher the score the more disposed the student is towards further study or engagement with mathematics)
<b>maths identity</b>	Statement2, 3, 6, 7, 11,12,14,15,16	This measure is constructed based on items that express mainly feelings and preferences towards mathematics (the higher the score the more positively/strongly the student relates or identifies with mathematics)
<b>maths self-efficacy</b>	Items in Appendix 2	Confidence in solving mathematical problems
<b>TeachingVariation</b>	Selected items from Lesson 1 to 26	The higher the score on this measure the more diverse the maths lessons from students' perspective
<b>TeachingTransmissionistScale</b>	Selected items from Lesson 1 to 26	The higher the score the more 'traditional' or teacher-centred the practices as reported by the students.

## INFORMATION RECEIVED FROM SCHOOLS

The following variables were collected either directly from schools for each of the students in our sample, or derived afterwards from the postcodes of student's address as also given from school. Please note that there are a lot of missing data in regards to these variables, firstly due to non-reporting from schools, and second due to inconsistency of the information given from schools.

There were cases within some schools where 'No's were explicitly stated and in others where it was left blank. This left us with little choice but to treat blanks as missing data.

Variable name	Description	Values/Categories
<b>suggested main</b>	This is our derived simplification of the extended and main ethnicity codes	Asian Black Chinese Information Not Yet Obtained Mixed Other OtherWhite Refused White
<b>extended</b>	These are the DCSF (Department for Children, Schools and Families) extended codes used for ethnicity <sup>1</sup>	Examples: AAFR (African Asian) ABAN (Bangladeshi) AIND (Indian) AKAO (Kashmiri other) AKPA (Kashmiri Pakistani) AMPK (Mirpuri Pakistani) ANEP (Nepali)
<b>main</b>	DCSF Main Code <sup>2</sup>	ABAN AIND AOTH APKN BAFR BCRB BOTH CHNE MOTH MWAS MWBA MWBC NOBT OOTH REFU WBRI WIRI WOTH
<b>fsm</b>	Free School Meal Eligibility	Y=Yes N = No
<b>sen_yn</b>	Whether the student has an SEN	Y = if school indicated SEN generally or by giving details N = if explicitly stated by school
<b>sen details</b>	SEN details for those with Yes in previous variable, when available	ASD = Autistic Spectrum Disorder BESD = Behaviour, Emotional & Social Difficulties HI = Hearing Impairment MLD = Moderate Learning Difficulty

<sup>1</sup> Detailed description is given at <http://www.communitycohesionncc.org.uk/docs/57.pdf>

<sup>2</sup> See <http://www3.hants.gov.uk/codes-ethnicbackgrounds.pdf> for descriptions

		MSI = Multi-Sensory Impairment OTH = Other Difficulty/Disability PD = Physical Disability PMLD = Profound & Multiple Learning Difficulty SLCN = Speech, Language and Communication Needs SLD = Severe Learning Difficulty SPLD = Specific Learning Difficulty VI = Visual Impairment
<b>first language</b>	Language of first choice	ENB = Not known but believed to be English ENG = English NOT = Information not obtained OTB = Not known but believed to be other than English OTH = Other than English PEN = Classification pending REF = Refused
<b>RANK OF IMD SCORE</b>	Index of Multiple Deprivation (IMD) rank is an index of wellbeing and deprivation based on postcode	Integer rank (1 is most deprived)
<b>Acorn Category<sup>3</sup></b>	Most broad category of demographics from Acorn classifications.	Affluent Achievers Comfortable Communities Financially Stretched Rising Prosperity Urban Adversity Not Private Households
<b>Acorn Group</b>	Acorn categories are divided into several groups	Career Climbers City Sophisticates Comfortable Seniors Countryside Communities Difficult Circumstances Executive Wealth Lavish Lifestyles Mature Money Modest Means Poorer Pensioners Starting Out Steady Neighbourhoods Striving Families Struggling Estates Student Life Successful Suburbs Young Hardship
<b>ACORN TYPE</b>	Demographic type code	1 to 62
<b>Acorn Type2</b>	Each group is also divided into more specific types.	Examples: Affluent professionals Asset rich families Better-off villagers <b>Note:</b> the whole list is presented in Appendix 5
<b>POLAR3qYPR</b>	Quintiles for young participation rate (Higher Education)	1=lowest participation 2 3 4 5=highest participation

<sup>3</sup> In **Appendix 5** we summarise the information from the Acorn types in a table.

## TEACHER-CLASS LEVEL DATASET

This dataset includes the responses to the teacher survey relevant to a particular class. The teachers were asked to complete this section for as many classes they teach (and take part in the student survey) which gives rise to multiple class occasions for the same teacher. They were also asked to do this at various times during the academic year (to ideally match data points 1 and 2 of the student surveys). Background information for the teachers is included in the 'teacher-level dataset'. The variables in the next table are identifiers and relevant to the class characteristics/information.

Variable name	Description	Values/Categories
<b>dp</b>	Data collection data point (as per student dataset)	1= DP1 2= DP2
<b>submit_date</b>	Data of completion	Date
<b>teacher_id</b>	Teacher id as per student dataset	Example: T0101
<b>school_id</b>	School ID as per student dataset	1 to 40
<b>class_id</b>	Class ID as per student dataset	Example: C01101
<b>dp_teacher_class</b>	A variable that combines the information for dp, teacher1_id and class_id. Useful for matching.	Example: 1T0108C01102
<b>year</b>	Year group of class	7 = Year 7 8 = Year 8 9 = Year 9 10 = Year 10 11 = Year 11 12 = Year 12
<b>number_of_students</b>	Number of students in class	Numeric value [3 to 34]
<b>class_changed</b>	[This was only asked at DP2]. Has this class changed since the beginning of the academic year?	1=yes 2=no
<b>class_changed_how</b>	If YES, please briefly describe how it changed:	OPEN
<b>only_teacher</b>	Are you the only teacher of this class?	1=yes 2=no
	Which of the following best describes the ability of the students in this class relative to the other students in this school?	
<b>class_ability</b>	Fairly homogeneous (setted) and low in ability [1] Fairly homogeneous (setted) and average in ability [2] Fairly homogeneous (setted) and high in ability [3] Mixed ability with two or more ability levels [4] Other setting, [5]	1 2 3 4 5
<b>class_ability_other</b>	If 'other' please describe:	OPEN
	Please indicate if any of the students in this mathematics class are formally classified as each of the following:	
<b>sen_1</b>	Specific learning difficulty (e.g. dyslexia, dyspraxia)	1 if ticked, else empty
<b>sen_2</b>	Other learning difficulties (e.g. moderate LD, autistic spectrum disorders)	2 if ticked, else empty
<b>sen_3</b>	Sensory and/or physical needs (hearing, visual etc.)	3 if ticked, else empty
<b>sen_4</b>	Behavioural, emotional and social difficulties	4 if ticked, else empty
<b>sen_5</b>	English as an Additional Language (EAL)	5 if ticked, else empty

The next table lists the items aiming to capture teaching practices. These were followed by the instruction “About how often do you do each of the following in your mathematics instruction in this class?” They were also used for the construction of the two measures (see later).

Variable name	Description	Values/Categories
teaching_1	I introduce a new topic by first determining what the students already know about it	1=Rarely 2=Sometimes 3=Often 4=Always
teaching_2	I offer content matter in gradually increasing levels of complexity	
teaching_3	I teach each topic from the beginning, assuming they know nothing	
teaching_4	I teach the whole class at once	
teaching_5	I jump between topics as the need arises	
teaching_6	I have my students work collaboratively in pairs	
teaching_7	I have my students work collaboratively in groups	
teaching_8	I teach each student differently according to individual needs	
teaching_9	I encourage students to discuss the mistakes they make	
teaching_10	I tend to follow the textbook closely	
teaching_11	Students work on projects in which subject material from various subjects is integrated	
teaching_12	Students decide for themselves whether it is necessary to cooperate with other students	
teaching_13	Students engage in mathematical activities using concrete materials	
teaching_14	Students make formal presentations to the rest of the class	
teaching_15	Students work on extended mathematics investigations or projects (a week or more in duration)	
teaching_16	Students start with easy questions and work up to harder questions	
teaching_17	Students read from a mathematics textbook in class	
teaching_18	Students use mathematical concepts to interpret and solve applied problems	
teaching_19	Students play mathematics games	
teaching_20	Students work through exercises from textbooks or worksheets	
teaching_21	Students work on their own, consulting a neighbour from time to time	
teaching_22	Students choose which questions to tackle	
teaching_23	I choose examples that appeal to students	
teaching_24	I try to indicate the value of each lesson topic for future use	
teaching_25	When a student asks a question, I give a clue (or scaffold) instead of the correct answer	
teaching_26	During instruction I ask a lot of short questions to check whether students understand the content matter	
teaching_27	I assign mathematics homework	
teaching_28	I ask students to explain their reasoning when giving an answer	
teaching_29	I encourage students to explore alternative methods for solutions	
teaching_30	I allow students to work at their own pace	

The variables in the following table were only asked at DP2 (therefore they are not included in the electronic copy of the survey).

Variable name	Description	Values/Categories
	How is the total overall teaching time spent for this class during this year? Please report the percentage for each general activity:	
<b>time_presentation</b>	Teacher talk/lesson presentation:	Percentage value
<b>time_individual_work</b>	Student work/talk:	Percentage value
<b>time_ts_interaction</b>	Teacher- student interaction:	Percentage value
<b>time_ss_interaction</b>	Student-student interaction:	Percentage value
<b>time_total</b>	Total time	100 (for all cases)

The final questions in the teacher survey, regarding the specific class, are listed below. The last two variables in the table are the constructed measures (using the teaching practice items presented in previous tables).

Variable name	Description	Values/Categories
	Think about your plans for this mathematics class for the entire year. How much emphasis will each of the following student objectives receive?	
<b>emphasis_1</b>	Increase students' interest in mathematics	1=Minimum 2=Moderate 3=Maximum
<b>emphasis_2</b>	Learn mathematical concepts	
<b>emphasis_3</b>	Learn mathematical algorithms/procedures	
<b>emphasis_4</b>	Develop students' computational skills	
<b>emphasis_5</b>	Learn how to solve problems	
<b>emphasis_6</b>	Learn how mathematics ideas connect with one another	
<b>emphasis_7</b>	Prepare for further study in mathematics	
<b>emphasis_8</b>	Learn to explain ideas in mathematics effectively	
<b>emphasis_9</b>	Learn how to apply mathematics in business and industry	
<b>emphasis_10</b>	Prepare students for standardized tests/exams	
<b>as_you_liked</b>	Has your teaching with this class been as you would like it to be?	1=Yes 2=No
<b>problems</b>	If NOT, please tell us what has been the main problems/barriers for this	OPEN
<b>other_comments</b>	Please give any other comments here:	OPEN
<b>Constructed measures with the Rasch Model :</b>		
<b>TVariation</b>	The higher the score the more varied the teaching practice with this class	In logit scale
<b>TTransmissionist</b>	The higher the score the more 'transmissionist' the teaching practice with this class	In logit scale



## TEACHER-LEVEL DATASET

This dataset includes the variables related to the particular teacher. They denote background information and were only asked once.

Variable name	Description	Values/Categories
<b>teacher_id</b>	Teacher ID for linking to student level data	
<b>school_id</b>	School ID	1-40
<b>gender</b>	The gender of the teacher	1=male 2=female
<b>ethnicity</b>	Ethnicity of the teacher 1 = White British 2 = White Irish 3 = Other White Background* 4 = Mixed - White and Black Caribbean 5 = Mixed - White and Black African 6 = Mixed - White and Asian 7 = Other Mixed Background* 8 = Asian or Asian British - Indian 9 = Asian or Asian British - Pakistani 10 = Asian or Asian British - Bangladeshi 11 = Other Asian Background* 12 = Black or Black British - Caribbean 13 = Black or Black British - African 14 = Other Black Background* 15 = Chinese 16 = Other Ethnic Background* 17 = Not known 18 = Prefer not to say	1-18
<b>ethnicity_other</b>	Further details on ethnicity	OPEN
<b>dob_year</b>	Year of birth of teacher	Integer
	Which of the following qualifications do you have? (tick all that apply)	
<b>quali_1</b>	Undergraduate degree in Maths (BA, BSc)	1
<b>quali_2</b>	Joint undergraduate degree in Maths and Other Subject	2
<b>quali_3</b>	Undergraduate degree in Education	3
<b>quali_4</b>	Undergraduate degree in Engineering	4
<b>quali_5</b>	Undergraduate degree in Science	5
<b>quali_6</b>	Other undergraduate degree*	6
<b>quali_7</b>	PGCE Secondary Mathematics	7
<b>quali_8</b>	Other PGCE course*	8
<b>quali_9</b>	Other postgraduate degree (MA, MSc, not PGCE)*	9
<b>quali_10</b>	Doctorate (PhD)	10
<b>quali_other</b>	Details of other degree qualification	OPEN
<b>no_course</b>	If they had never taken a mathematics course	1=Never
<b>years_teaching</b>	Number of years teaching	Integer
<b>In the last 2 years, have you received training in these areas from any source or taken part in any of the activities?</b>		
<b>training_1</b>	Trained in the use of computers and technology	1=Yes 2=No
<b>training_2</b>	Trained in the integration of computers and other technology into the classroom curriculum	

<b>training_3</b>	Follow-up or advanced training	
<b>training_4</b>	Taught any in-service workshops in mathematics or mathematics teaching?	
<b>training_5</b>	Mentored another teacher as part of a formal arrangement that is recognized or supported by the school or district, not including supervision of student teachers?	
<b>training_6</b>	Received any grants or awards for mathematics teaching?	
<b>training_7</b>	Served on a school or local authority mathematics curriculum committee?	
<b>training_other</b>	Other training they have received	OPEN
<b>When students are successful in achieving intended goals or objectives, it is often attributed to one of the following sources. In your opinion, how important is each source of success?</b>		
<b>importance_1</b>	Student's home background	1=Unimportant
<b>importance_2</b>	Student's intellectual ability	2=Important
<b>importance_3</b>	Student's enthusiasm or perseverance	3=Very important
<b>importance_4</b>	Teacher's attention to the unique interests and abilities of the student	
<b>importance_5</b>	Teacher's use of effective methods of teaching	
<b>importance_6</b>	Teacher's enthusiasm or perseverance	
<b>can_learn_maths</b>	Most people can learn to be good at math	1 = Strongly disagree
<b>born_maths_ability</b>	You have to be born with the ability to be good at math	2 = Disagree
		3 = Unsure
		4 = Agree
		5 = Strongly agree

## REFERENCES

- Andrich, D. (1999). Rating Scale Model. In G. N. Masters & J. P. Keeves (Eds.), *Advances in Measurement in Educational Research and Assessment* (pp. 110 - 121). Oxford: Pergamon.
- Bond, T., & Fox, C. M. (2001). *Applying the Rasch Model: Fundamental Measurement in the Human Sciences*. Mahwah, NJ: Lawrence Erlbaum.
- Messick, S. (1988). The Once and Future Issues of Validity: Assessing the Meaning and Consequences of Measurement. In H. Wainer & H. I. Braun (Eds.), *Test Validity* (pp. 33-45). London: Lawrence Erlbaum Associates, Publishers.
- Messick, S. (1989). Validity. In R. L. Linn (Ed.), *Educational Measurement* (Third ed., pp. 13-103). USA: American Council of Education and the Oryx Press.
- Pampaka, M., Williams, J., & Hutchenson, G. (2012). Measuring students' transition into university and its association with learning outcomes. *British Educational Research Journal*, 38(6), 1041-1071.
- Pampaka, M., Williams, J. S., Hutcheson, G., Wake, G., Black, L., Davis, P., & Hernandez - Martinez, P. (2012). The association between mathematics pedagogy and learners' dispositions for university study. *British Educational Research Journal*, 38(3), 473-496.
- Pampaka, M., & Wo, L. (2014). *Revisiting Mathematical Attitudes of students in Secondary Education*. In Liljedahl, P., Oesterle, S., Nicol, C., & Allan, D. (Eds.) *Proceedings of the Joint Meeting of PME 38 and PME-NA 36, Vol. 4, pp. 385-392*. . Paper presented at the The Joint Meeting of PME 38 and PME-NA 36, Canada, Vancouver.
- Thissen, D., Steinberg, L., & Wainer, H. (1993). Detection of Differential Item Functioning Using the Parameters of Item Response Models. In P. W. Holland & H. Wainer (Eds.), *Differential Item Functioning* (pp. 67-114). London Lawrence Erlbaum Associates, Publishers.
- Wolfe, E. W., & Smith Jr., E. V. (2007a). Instrument Development Tools and Activities for Measure Validation Using Rasch Models: Part I - Instrument Development Tools. *Journal of Applied Measurement*, 8(1), 97-123.
- Wolfe, E. W., & Smith Jr., E. V. (2007b). Instrument Development Tools and Activities for Measure Validation Using Rasch Models: Part II - Validation Activities. *Journal of Applied Measurement*, 8(2), 204-234.
- Wright, B. D., & Masters, G. N. (1982). *Rating Scale Analysis*. Chicago: MESA Press.
- Wright, B. D., & Mok, M. (2000). Rasch Models Overview. *Journal of Applied Measurement*, 1(1), 83-106.

### APPENDIX 1 – EXAMPLE INVITATION LETTER

Dear Teacher/Headteacher,

Would your school be interested in participating in a research project looking at improving maths teaching in secondary schools? If you would like to be involved in the project, then please contact me via email. Equally, if you would like to hear more about the project before making a decision, we would be very happy to visit you to talk in more depth about it, so please let us know. The project will begin in September 2011.

There is also a pilot stage in June 2011, mainly for testing our questionnaires and online survey tool, so please let us know if you would also be happy for us to pilot the survey in your school.

In short, the project is about secondary school mathematics teaching and learning (more details attached). We aim to map pedagogy and learner outcomes across a range of schools, through an (online) survey of students and teachers, which we plan for the next academic year (2011-12). In particular, we hope to collect data from students in Year 7 to Year 11 three times a year (1. At the beginning of academic year 2011-12, 2. Towards the end of the same academic year, and 3. At the beginning of the following academic year) to be able to map their progression in mathematics. At the same time, we are hoping to collect teachers' perceptions about their teaching with these students during the first year of the project.

In terms of impacting on maths pedagogy in your school, we are confident that with this design we will be able to help your school collect evidence of what is working in mathematics pedagogy, where, and why. You can have access to your school's data (of course conforming with the ethical assumptions of anonymity and confidentiality) and also our general results which will inform on students' attitudes to mathematics and their association with the reported pedagogical experience. In addition, there is going to be opportunities to join a network of mathematics teachers discussing these results (with at least two events sponsored from the projects and others to be negotiated).

In addition to the questionnaires, we also plan to have mini case studies in some schools, with interviews and observations of mathematics lessons. This will be decided once the project is underway but if you think you might be interested in this part of the research then please also let us know.

We are sending out this letter to all the secondary head teachers/mentors of PGCE students at the University X as we know many of you have worked closely with some of our colleagues from the School of Education on other occasions.

I look forward to hearing from you and please do not hesitate to contact me if you have any queries.

Kind regards

Maria

## APPENDIX 2 – THE MATHEMATICS SELF EFFICACY ITEMS

The list presented here is to help match the items with the final dataset, and we thus present them in this order. It may be useful for some users to also draw on the particular questionnaires (hard copies) for each of the year group and data point.

This section was always starting with the following instructions:

### Part E- How confident are you with different topics in mathematics?

In this section, we are asking you to say how confident you would be at using mathematics to solve different problems. We don't ask you to actually solve the problems.

Imagine that you have been given the following questions to do. You would be able to use your notes, textbooks, calculator, and so on when necessary. Please tell us how confident you are that you would be able to solve each problem, without actually doing the problem.

How confident are you that you are able to solve problems of the kind given in each case?

Please circle one response for each task.

## MSE1

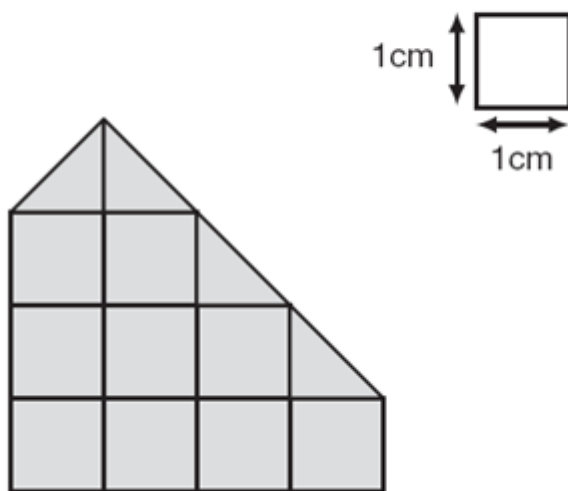
Mike asked his friends which feature they used most on their mobile phones. He recorded the results in a tally table.

- (a) Complete the frequency column in the table below.  
The first two values are done for you.

Feature	Tally	Frequency
Phone calls	HHH II	7
Texts	III	3
Photos	HHH HHH II	
Internet	HHH HHH	
Games	IIII	

## MSE2

What is the **area** of the shaded shape in square centimetres?



## MSE3

Calculate  
 $(-24) \div (+6)$

## MSE4

Calculate  
 $(-6) - (+3)$

## MSE5

A brother and sister have a total age of 20 years.  
The brother is aged  $n$  years old.  
Circle the expression for the sister's age.

$n - 20$      $n + 20$      $20 - n$      $20n$      $20 / n$

## MSE6

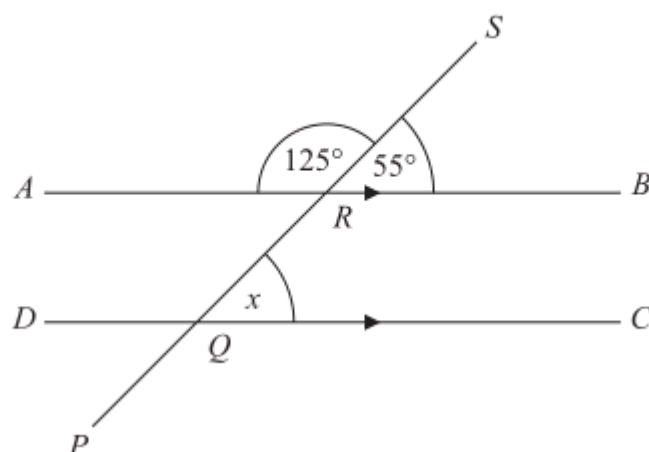


Diagram **NOT**  
accurately drawn

$ARB$  is parallel to  $DQC$ .

$PQRS$  is a straight line.

Angle  $SRB = 55^\circ$ .

(i) Find the size of the angle marked  $x$ .

.....

## MSE7

The  $n$ th term of a number sequence is given by  $3n + 1$

(a) Work out the first **two** terms of the number sequence.

.....  
(1)

## MSE8

Here are the first four terms of another number sequence.

1      5      9      13

(b) Find, in terms of  $n$ , an expression for the  $n$ th term of this number sequence.

.....  
(2)

## MSE9

Here are the ages, in years, of 16 people.

36	48	18	25	36	28	45	30
38	27	41	16	36	48	28	21

(b) Find the median age.

..... years  
(2)



## MSE10

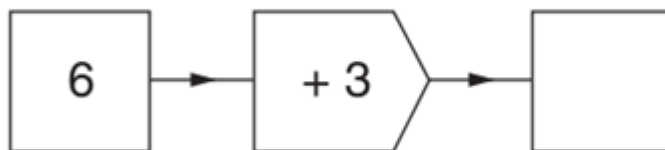
Mr Gordon pays for a family holiday.

(a) Complete his bill.

Description	Cost
2 adults @ £540 each	
3 children @ £250 each	
Hire of car for 10 days @ £20 per day	
Total	£

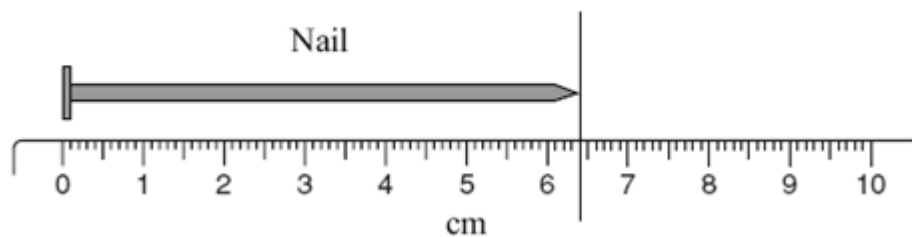
## MSE11

Complete the number machine calculation by filling in the empty box.

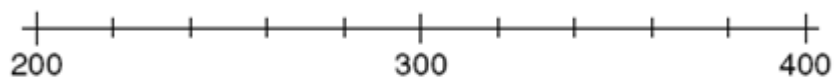


## MSE12

How long is the nail?



### MSE13



On this number line, mark the position of 270.

### MSE14

$PQR$  is a right-angled triangle.

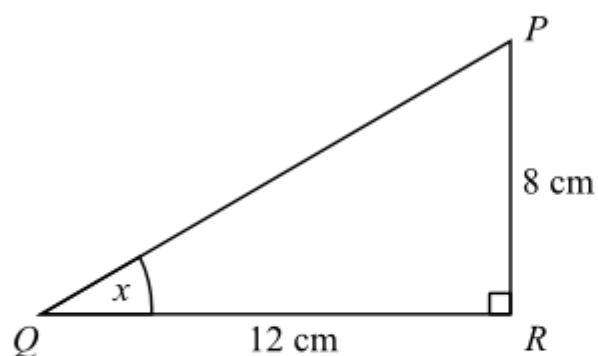


Diagram **NOT**  
accurately drawn

$PR = 8\text{ cm}$ .

$QR = 12\text{ cm}$ .

Find the size of the angle marked  $x$ .

Give your answer correct to 1 decimal place.

## MSE15

This frequency table gives information about the ages of 60 teachers.

Age ( $A$ ) in years	Frequency
$20 < A \leq 30$	12
$30 < A \leq 40$	15
$40 < A \leq 50$	18
$50 < A \leq 60$	12
$60 < A \leq 70$	3

a) Complete the cumulative frequency table.

Age ( $A$ ) in years	Cumulative frequency
$20 < A \leq 30$	
$30 < A \leq 40$	
$40 < A \leq 50$	
$50 < A \leq 60$	
$60 < A \leq 70$	

## MSE16

In a quiz there are ten questions.

Each correct answer gains five points.

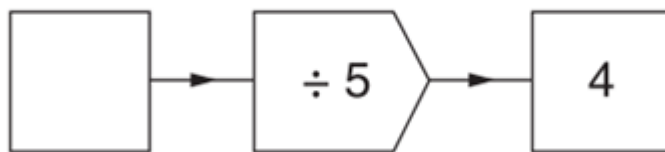
Each wrong answer loses two points.

Glen gave seven correct answers and three wrong answers.

How many points did he get altogether?

## MSE17

Complete the number machine calculation by filling in the empty box.



## MSE18

Simplify  $2x + 8 + 4x - 3$

## MSE19

Solve this equation

$$\frac{x}{3} = 5$$

## MSE20

Calculate 36% of £420.

## MSE21

Complete the table of values for  $y = 3x + 4$

$x$	0	1	2	3	4	5
$y$	4		10		16	19

## MSE22

Calculate  $\frac{4.5}{0.6^2}$

## MSE23

Work out  $4\frac{1}{5} - 1\frac{2}{3}$

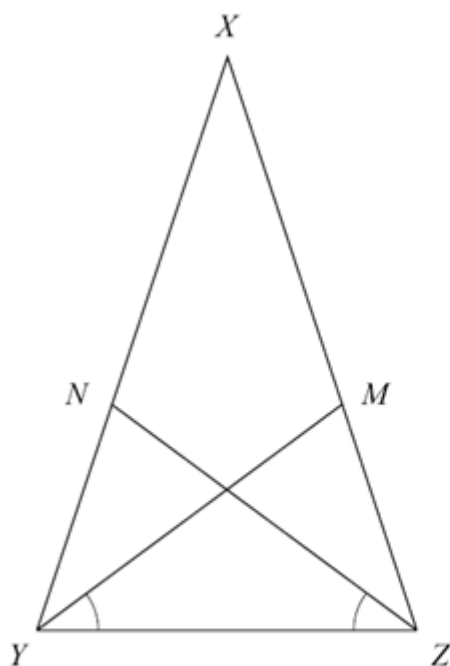
## MSE24

Simplify  $\frac{2(x+3)^2}{8(x+3)}$

## MSE25

$XYZ$  is an isosceles triangle in which  $XZ = XY$

$M$  and  $N$  are points on  $XZ$  and  $XY$  such that angle  $MYZ$  = angle  $NZY$



Prove that triangles  $YMZ$  and  $ZNY$  are congruent.

## MSE26

Aidan puts 2 white counters and 1 black counter in a bag.

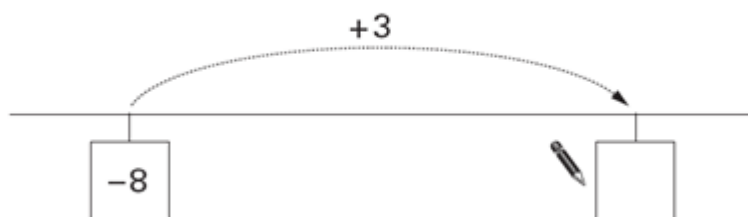


He is going to take one counter without looking.

What is the **probability** that the counter will be **black**?

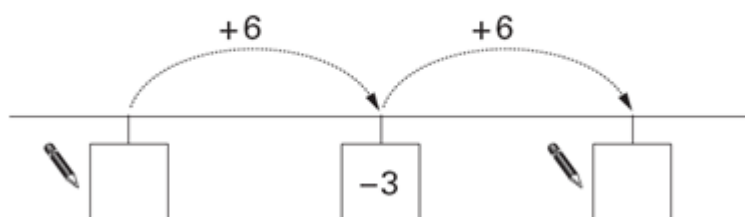
## MSE27

Write the missing number on the number line



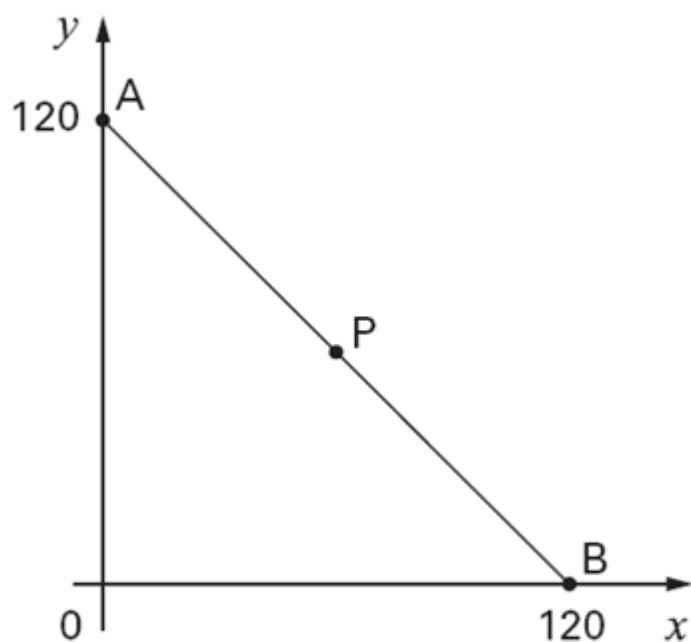
## MSE28

Write the missing numbers on the number lines



## MSE29

P is the **midpoint** of line AB.



What are the coordinates of point **P**?

## MSE30

(a) Write the number 4117 in words.

..... (1)


(b) Write the number 4117 to the nearest hundred.

..... (1)

## MSE31

Put these times in order, starting with the shortest.

5 minutes      20 seconds      100 seconds      1 minute




shortest

## MSE32

Here is a number chart.

Circle the **smallest** number on the chart that is a multiple of **both 2 and 7**



71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



## MSE33

Here are four digit cards.



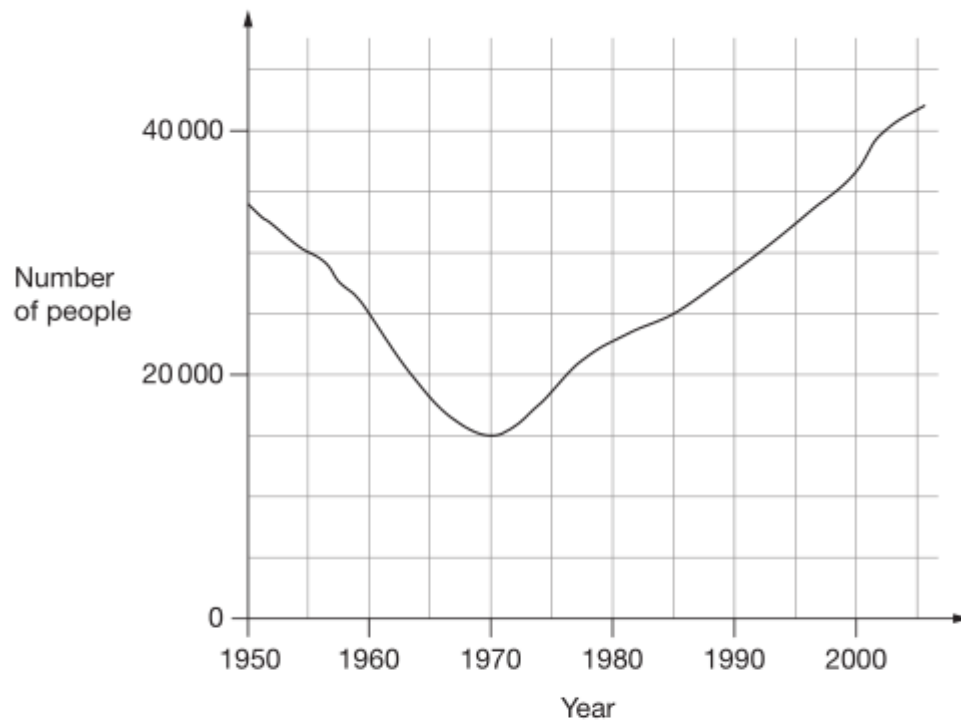
Use each digit card **once** to make the decimal number **nearest to 20**



## MSE34

20

This graph shows the number of people living in a town.



Look at the graph.

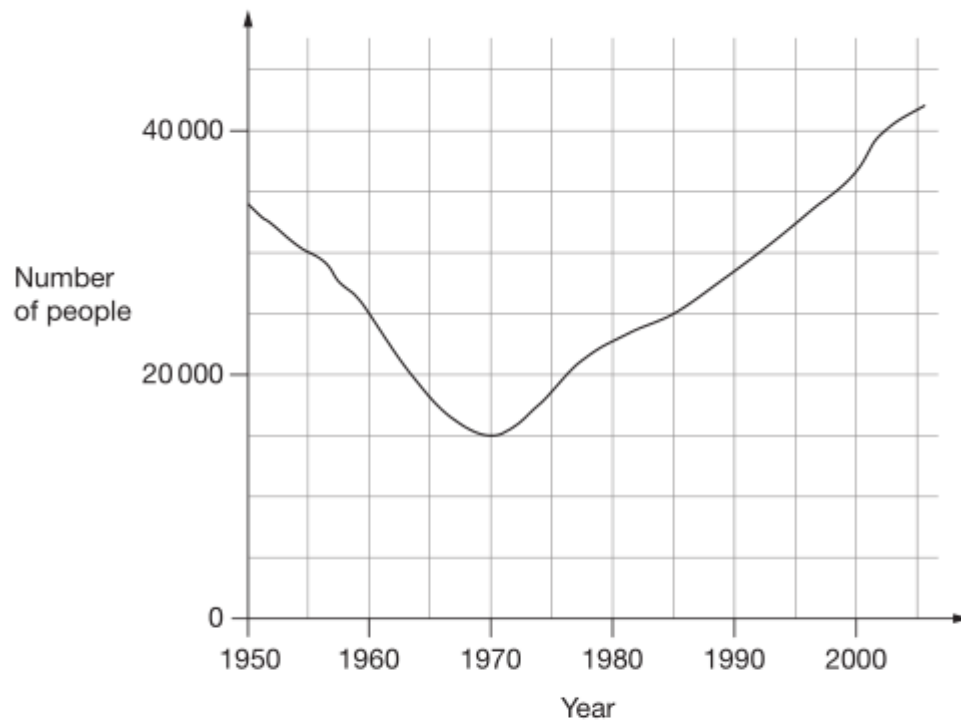
How many people lived in the town in 1985?



## MSE35

20

This graph shows the number of people living in a town.



Look at the graph.

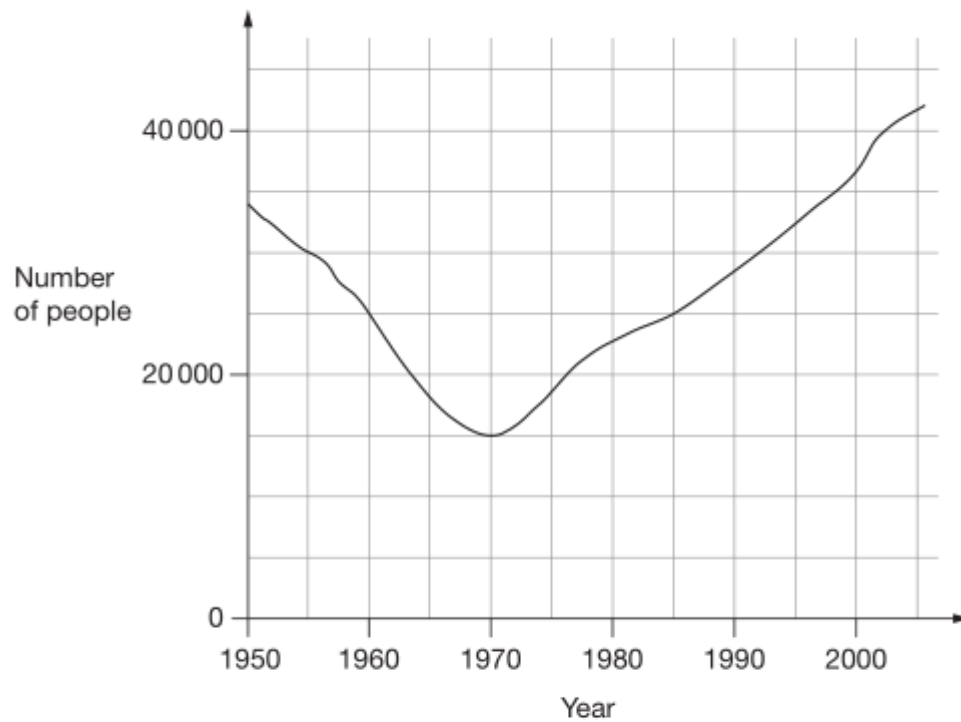
In which year was the number of people the same as in 1950?



## MSE36

20

This graph shows the number of people living in a town.



Look at the graph.

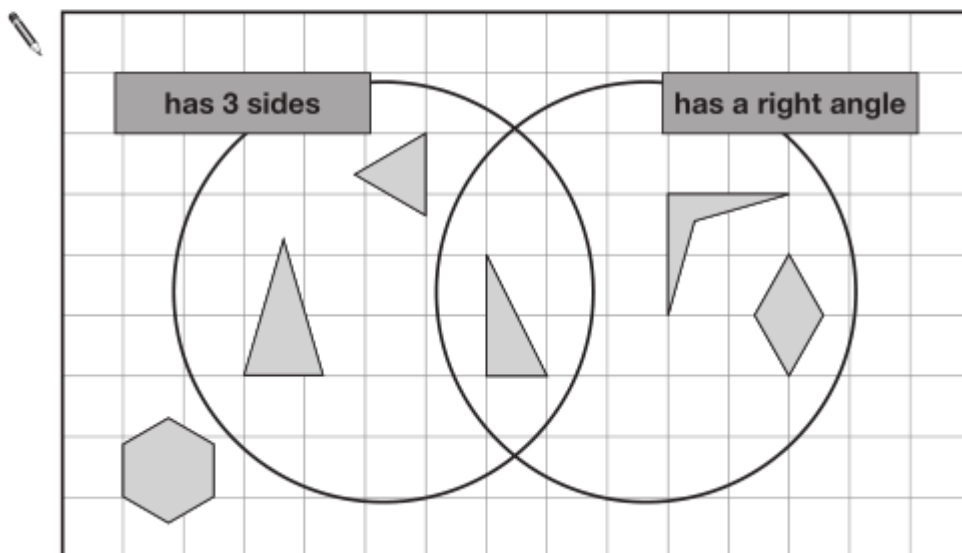
Find the year when the number of people first went below 20 000



## MSE37

Here is a diagram for sorting shapes.

One of the shapes is in the wrong place.  
Put a cross (✕) on it.



## MSE38

Emily has these coins.



How much more money does Emily need to make exactly £5?

 £

## MSE39

Amir says,

***'All numbers that end in a 4  
are multiples of 4'.***



Is he correct?  
Circle **Yes** or **No**.

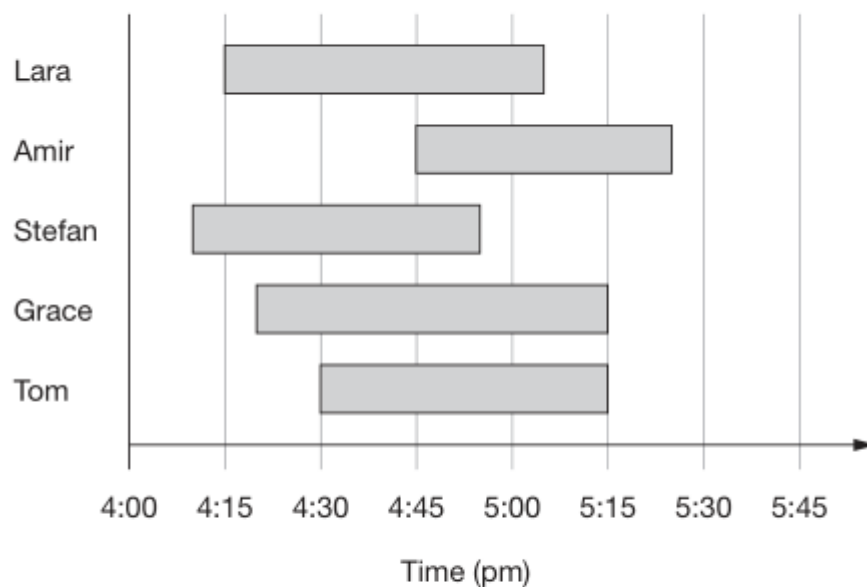
 Yes / No

Explain how you know.

A large, empty, cloud-shaped box with a scalloped border, intended for the student to write their explanation.

## MSE40

This chart shows the times when 5 children were at a swimming pool one afternoon.



Who was the next person to arrive after Stefan?

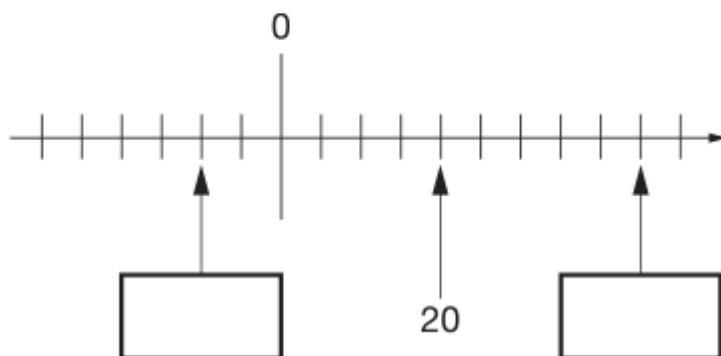


\_\_\_\_\_

## MSE41

Here is part of a number line.

Write the missing numbers in the boxes.



## MSE42

Stefan has a bag that contains 3 blue marbles and 5 red marbles only.



What fraction of the marbles in the bag are blue?



## MSE43

13

Liam thinks of a number.

He divides it by 9 and then adds 25 to the result.

His answer is 36



What number did Liam start with?

Show your **method**.  
You may get a mark.



## MSE44



$$\frac{1}{u} + \frac{1}{v} = \frac{1}{f}$$

$$u = 2\frac{1}{2}, v = 3\frac{1}{3}$$

- (a) Find the value of  $f$ .

## MSE45

A rugby team played 7 games.

Here is the number of points they scored in each game.

3      5      8      9      12      12      16

- (a) Work out the range.

.....  
(2)

## MSE46

Solve the equation:

$$(x + 3)(2x - 4) = 5$$

## MSE47

Here is a list of ingredients for making **8** cheese scones.

**Ingredients for 8 cheese scones**

200 g self-raising flour

60 g butter

30 g cheese

150 ml milk

Work out the amount of each ingredient needed to make **12** cheese scones.

..... g self-raising flour

..... g butter

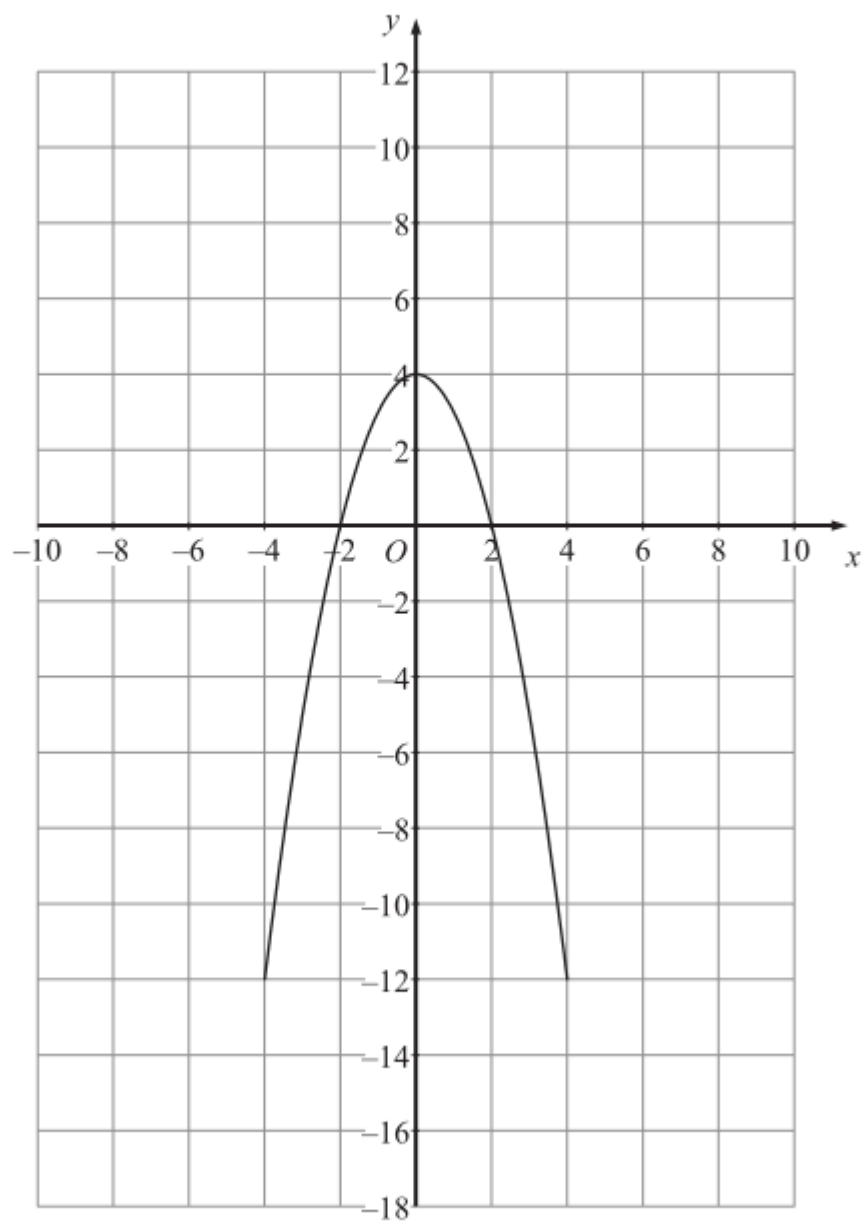
..... g cheese

..... ml milk

**MSE48**

The graph of  $y = f(x)$  is shown on the grids.

(a) On this grid, sketch the graph of  $y = f(x) - 4$



**MSE49**

Here is a picture of Fred standing outside his house.



- (a) Which measurement below is most likely to be **Fred's height**?

Put a ring round the correct answer.



0.8 metres

1.8 metres

2.8 metres

3.8 metres

## MSE50

Here is a picture of Fred standing outside his house.



- (b) Which measurement below is most likely to be the **height** of **Fred's house**?

Put a ring round the correct answer.



1 metre

7 metres

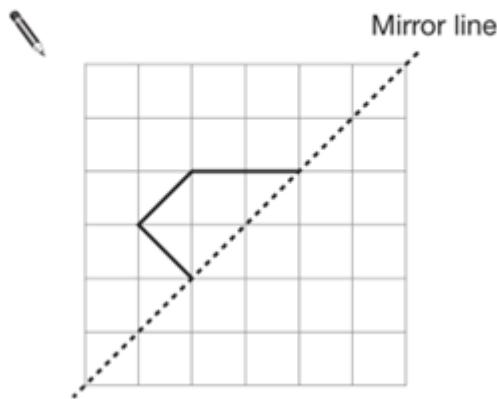
17 metres

27 metres

## MSE51

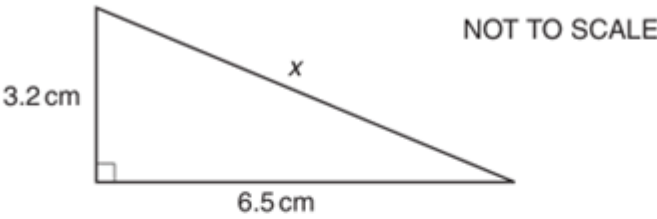
The diagrams in this question are drawn on square grids.

Reflect the shape in the mirror line.



MSE52

Calculate the value of  $x$ .



.....

.....

.....

.....

.....

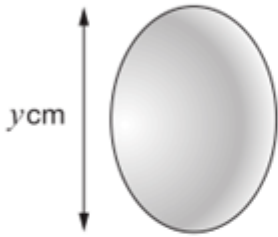
.....

\_\_\_\_\_ cm [3]

MSE53

In this question you will need the following information about hens' eggs.

Approximate **mass**, in grams, is given by:

$$\text{Mass} = \frac{\pi y^3}{10} \times 1.15$$


Mass of egg	Grade of egg
Up to 53g	Small
53g up to 63g	Medium
63g up to 73g	Large
73g or more	Extra large

The length,  $y$ , of an egg is **5.5cm**.

Use the formula to find the **grade** of the egg.

You **must** show your working.



Grade \_\_\_\_\_

MSE54

A dessert has both fruit and yoghurt inside.



**Altogether**, the mass of the fruit and yoghurt is **175g**.

The **ratio** of the mass of **fruit** to the mass of **yoghurt** is **2 : 5**

What is the mass of the yoghurt?

\_\_\_\_\_ g

## MSE55

Each rule below makes a sequence.

Use the rule to write the **next two numbers** for each sequence.

Rule: <b>Add 3</b> to the last number				
2	5	8	_____	_____

## MSE56

Each rule below makes a sequence.

Use the rule to write the **next two numbers** for each sequence.

Rule: <b>Double</b> the last number then <b>add 1</b>					
2	5	11	_____	_____	

## MSE57

Each rule below makes a sequence.

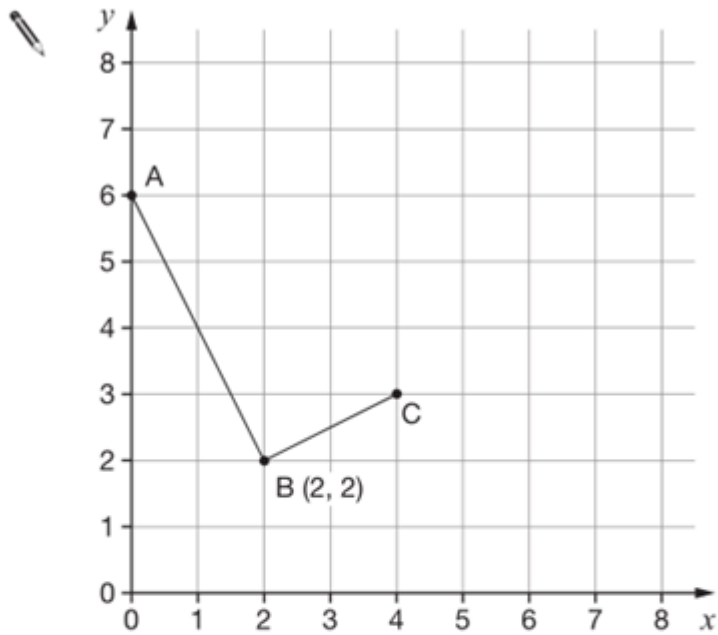
Use the rule to write the **next two numbers** for each sequence.

Rule: <b>Multiply</b> the last number <b>by 3</b> then <b>subtract 1</b>					
2	5	14	_____	_____	

## MSE58



Look at the graph.



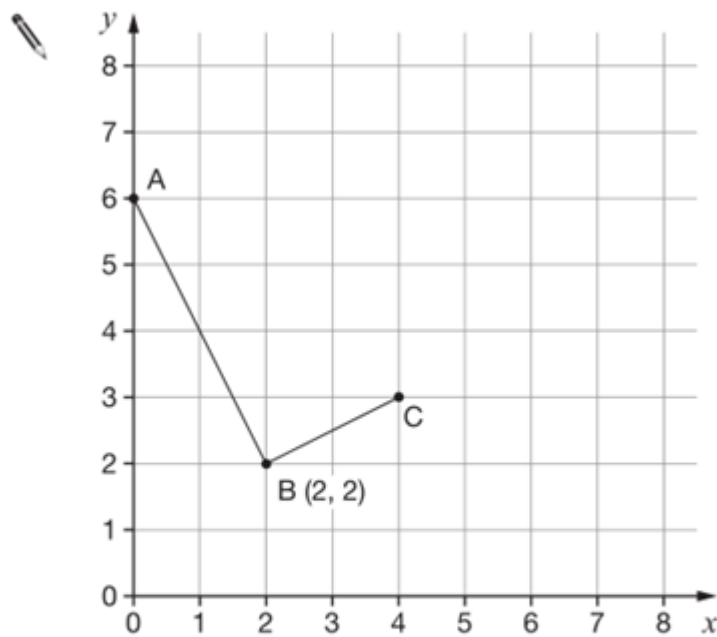
Write down the coordinates of points A and C.

 A is ( \_\_\_\_\_ , \_\_\_\_\_ )

C is ( \_\_\_\_\_ , \_\_\_\_\_ )

**MSE59**

Look at the graph.



Point D can be marked so that ABCD is a **rectangle**.

Mark point D accurately on the graph.

MSE60

The table shows some information about five children.

Name	Gender	Age	Hair Colour
Aaron	Male	6	Black
Becky	Female	10	Brown
Kim	Female	6	Brown
Darren	Male	9	Blonde
Emily	Female	4	Red

(a) Write down the colour of Darren’s hair.

.....

## MSE61

The pie chart shows the sports played by 60 students during their games lesson.



- (a) How many students play football?

.....

Answer .....

## MSE62

Here is some information about class 7J.

There are 30 pupils altogether.

There are 2 more girls than boys.

A quarter of the girls are left-handed.

There are 7 left-handed pupils altogether.

Use this information to complete the two-way table below.

	Boys	Girls	Total
Left-handed			
Right-handed			
Total			30

## MSE63

Mr. and Mrs. Jackson are going to an exhibition with their two children, Abby and Ben.

They see this price list.

Ticket type	Cost
Children (under 6)	free
Children (under 18)	£2.25
Adults	£5.25
Family ticket (up to 2 adults and 2 children)	£12

Abby is 6 years old and Ben is 12 years old.

Calculate how much the family saves by buying a family ticket instead of separate tickets.



£

## MSE64

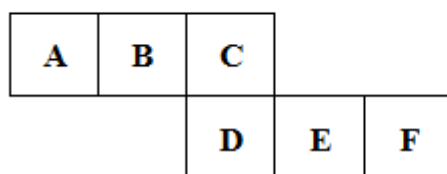
A clock shows 12 noon.

Through how many degrees does the **hour hand** turn in an hour?



## MSE65

A net for making a cube is shown below.

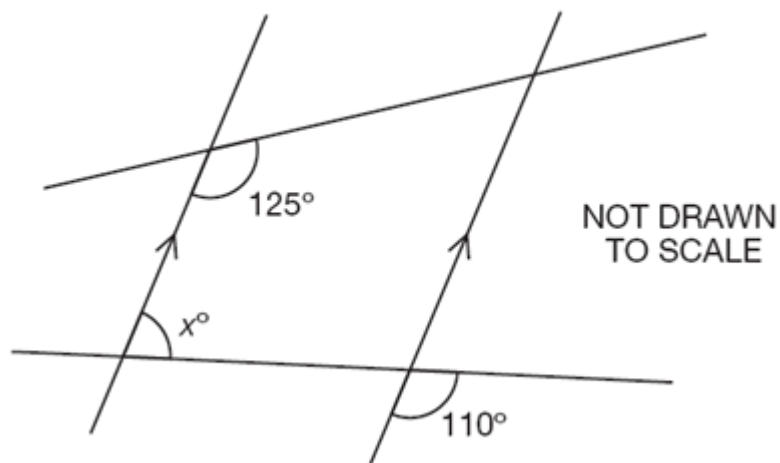


When folded up, which face is **opposite** D?



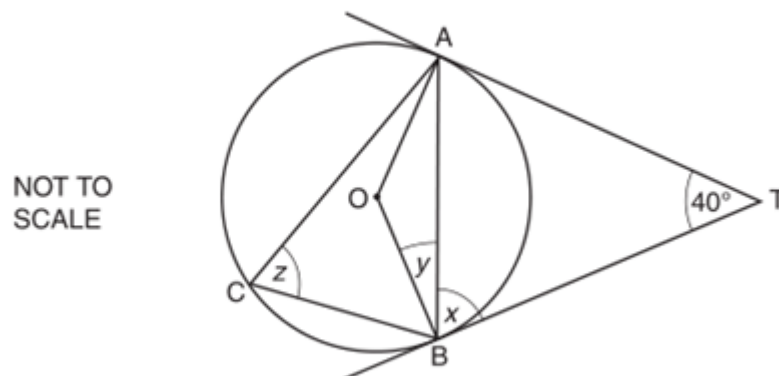
## MSE66

Calculate angle  $x$ .



## MSE67

A, B and C are points on a circle, centre O.  
TA and TB are tangents to the circle.  
Angle  $ATB = 40^\circ$ .



- (a) Find angle  $x$ .  
Give a reason for your answer.

Calculate which coach journey is better value in terms of pence per mile.

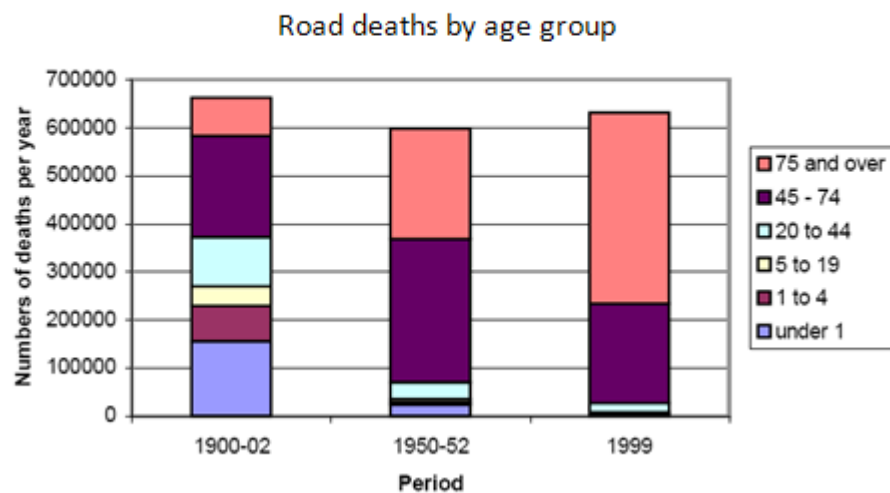
Birmingham – London, 110 miles, cost £14.50

Oxford – Leeds, 170 miles, cost £24.60

## MSE68

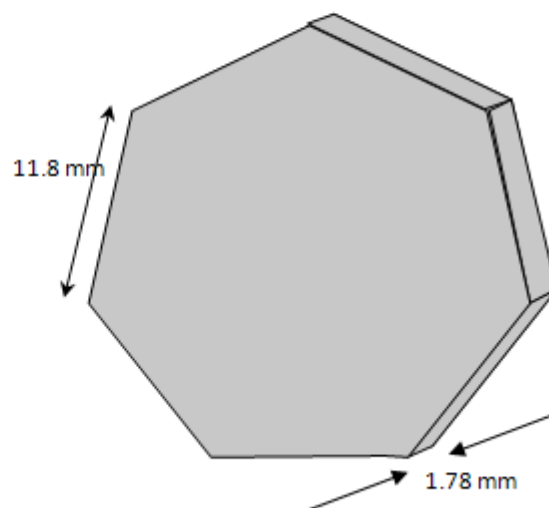
## MSE69

Interpret the graph below to describe how road casualties of some different age groups have changed over time.



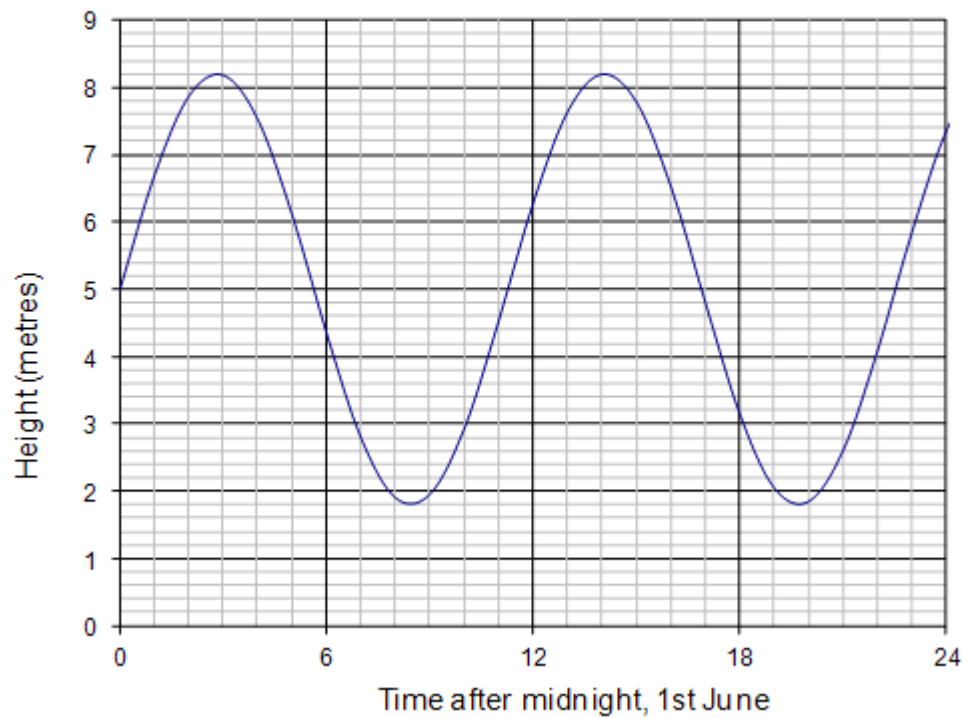
## MSE70

A 50 pence piece can be modelled as a prism with a regular seven sided figure as its cross section. Using the dimensions in the diagram calculate an estimate for the volume of metal in a 50 pence piece.



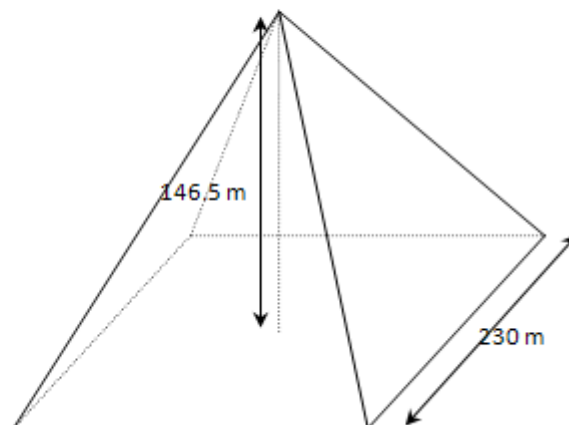
## MSE71

The graph below of the height of water during one complete day at Fleetwood, on the Lancashire coast, shows that the time between high tides is not exactly twelve hours. Estimate the **times** of high and low tides one week after the day shown on this graph.



## MSE72

The Great Pyramid at Giza in Egypt has dimensions as shown in the diagram. Find the angle that a triangular face makes with its (square) base.



## MSE73



Assume that on average house prices rise 7% every year.

A house is valued at  $\pounds V$  now.

By writing down a formula, in terms of  $V$ , that will allow you to estimate the future value,  $\pounds V(t)$ , of a house in  $t$  years time, find the expected value of a house in 15 years time if it is valued at  $\pounds 175000$  now.

## MSE74

Use the information below to calculate the cost of a holiday for a group of six travellers. There are two couples and two single travellers in the group. They wish to start the main holiday on August 5<sup>th</sup>, with one couple and one single traveller extending the holiday for 7 nights in Sorrento in a room with a sea view and with half board.

2006 - Saturdays

per person in a twin room

Date	Price	Date	Price	Date	Price	Date	Price
Apr 8	£845	Jun 3	£875	Jul 29	£755	Sep 23	£865
Apr 15	£845	Jun 10	£875	Aug 5	£745	Sep 30	£865
Apr 22	£855	Jun 17	£855	Aug 12	£775	Oct 7	£875
Apr 29	£855	Jun 24	£855	Aug 19	£775	Oct 14	£855
May 6	£865	Jul 1	£745	Aug 26	£775	Oct 21	£845
May 13	£865	Jul 8	£745	Sep 2	£875		
May 20	£855	Jul 15	£735	Sep 9	£875		
May 27	£855	Jul 22	£735	Sep 16	£865		

**Price Includes**  
Air travel, UK departure taxes, overseas airport taxes, all transportation, breakfast daily, dinner on days 4 & 7, itinerary as described, tour escort and official city guides, guidebook

**Not Included**

Supplements per person	
Supplement	Price
Single supplement	£170

Extension	
7-nights Sorrento	Price
Grand Hotel Vesuvio	£375
(Aug - Oct)	£425
Single supplement	£70
Sea view	£75
Half board (lunch or dinner)	£50
Sea view	£75

## MSE75

The table gives the lengths of rivers in metres but expressed in different ways.  
Put these rivers in decreasing order of length.

River	Length
Amazon	$6.39 \times 10^6$ metres
Yellow	$4.67 \times 10^9$ millimetres
Nile	6690000000 millimetres
Yangtze	6380 kilometres
Congo	4371000 metres
Mississippi	$6.27 \times 10^6$ kilometres

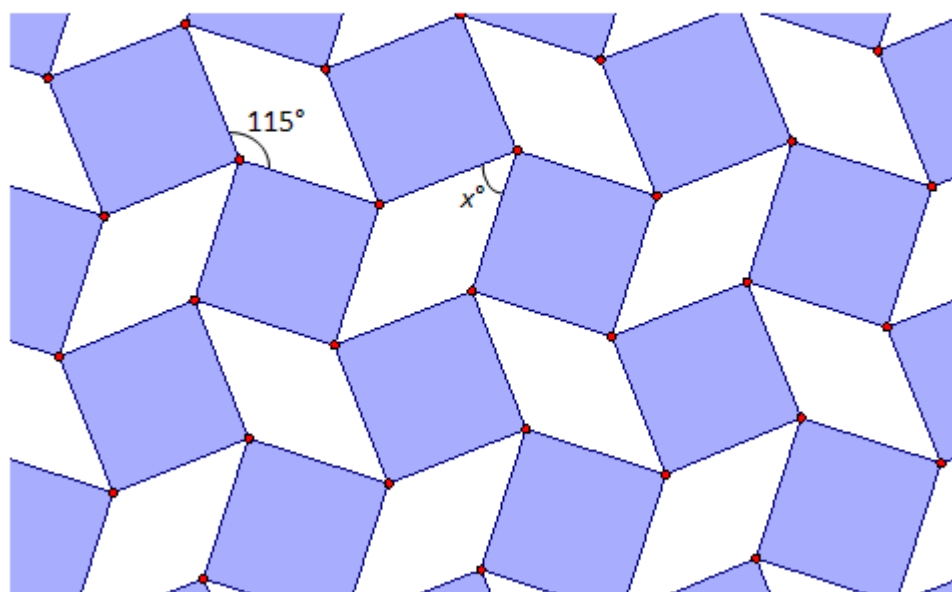
## MSE76

Solve for  $x$ :

$$15 - 2x = 3x + 25$$

## MSE77

The diagram shows a tiling pattern formed by tessellating squares and parallelograms.  
Find the angle marked  $x^\circ$ .



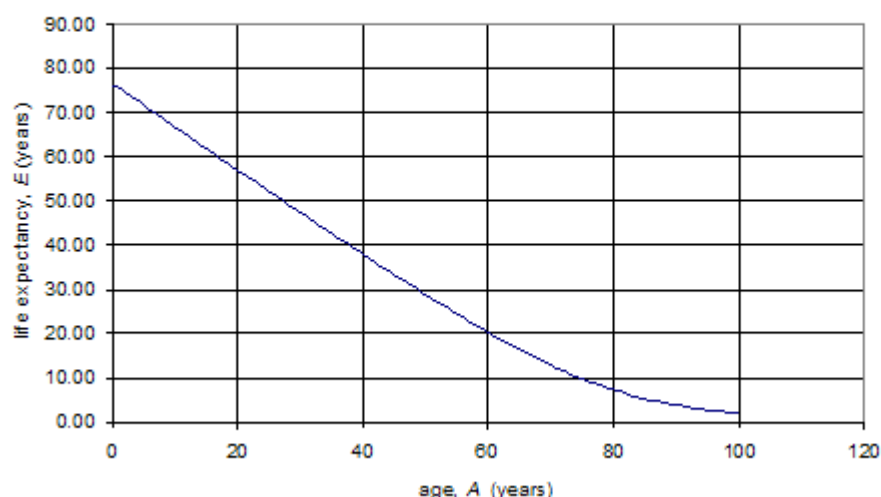
## MSE78



A golfer hits a ball so that its height,  $h$  metres, above horizontal ground is given by  $h = 20t - 5t^2$ .  
Find when the ball is 5 metres above the ground by solving  $5 = 20t - 5t^2$ .

## MSE79

The graph below shows how male life expectancy,  $E$  years, varies with age,  $A$  years.  
Find a linear formula connecting  $E$  and  $A$  for males aged between 0 and 60 years.



## APPENDIX 3 – MSE ITEMS BY DATA POINT AND YEAR GROUP

There were the occasional small differences between online and hard copy items and the items were also presented in slightly different orders to:

1. manage efficient use of space in the hard copies between long and short items and to
2. make it easier for the online survey to manage the different routes through the MSE items (depending on year group)

Items given at each year group, at **DP1**:

item	Y7	Y8	Y9	Y10	Y11
MSE11	x				
MSE17	x	x			
MSE38	x				
MSE42	x				
MSE33	x				
MSE21	x				
MSE27	x	x			
MSE31	x				
MSE41	x				
MSE51	x	x	x		
MSE2	x				
MSE60	x	x			
MSE40	x	x			
MSE37	x	x	x		
MSE26	x	x	x		
MSE62	x	x			
MSE49	x	x	x		
MSE50				x	x
MSE55	x				
MSE56		x			
MSE57			x		
MSE30		x	x		
MSE63		x	x	x	
MSE39		x	x	x	x
MSE1		x			
MSE45	x	x	x	x	x
MSE13		x	x	x	x
MSE19		x	x		
MSE34	x				
MSE35		x	x		
MSE36				x	x
MSE47		x	x	x	x
MSE58		x	x	x	

item	Y7	Y8	Y9	Y10	Y11
MSE59		x		x	
MSE4		x	x		
MSE10			x	x	
MSE16			x	x	
MSE32			x	x	
MSE23			x	x	x
MSE61				x	x
MSE3				x	x
MSE20				x	x
MSE25				x	x
MSE53				x	x
MSE48				x	x
MSE66				x	
MSE18				x	
MSE67					x
MSE24					x
MSE43					x
MSE52					x
MSE44					x
MSE74					x
MSE75					x
MSE76				x	x
MSE69				x	x

Items given at each year group, at **DP2**:

item	Y7	Y8	Y9	Y10	Y11
MSE38	x				
MSE30	x				
MSE42	x				
MSE31	x				
MSE2	x				
MSE27	x	x			
MSE21	x	x	x		
MSE13	x	x	x	x	
MSE45	x	x	x	x	
MSE26	x	x	x		
MSE12	x	x	x		
MSE17	x	x			
MSE40	x	x			
MSE49	x	x			
MSE35	x	x			
MSE60	x	x			
MSE51	x	x	x		

item	Y7	Y8	Y9	Y10	Y11
MSE33	x	x	x	x	
MSE64	x	x	x	x	
MSE4	x	x	x	x	
MSE23	x	x	x	x	x
MSE47				x	x
MSE61				x	
MSE19		x			
MSE29		x	x		
MSE63		x	x	x	
MSE39		x	x	x	
MSE58		x	x	x	
MSE10			x	x	
MSE36			x	x	x
MSE20			x	x	x
MSE76			x	x	x
MSE25			x	x	x
MSE3		x	x	x	x
MSE54		x	x	x	
MSE65		x	x	x	
MSE5		x	x	x	
MSE22		x	x	x	
MSE66			x	x	
MSE53			x	x	x
MSE69				x	x
MSE48				x	x
MSE44				x	x
MSE50					x
MSE67					x
MSE24					x
MSE43					x
MSE75					x
MSE77					x
MSE78					x
MSE72					x
MSE6					x
MSE7					x
MSE8					x
MSE9					x
MSE15					x
MSE14					x

Items given at each year group, at **DP3**:

item	Y7	Y8	Y9	Y10	Y11	Y12
MSE11	x					
MSE38	x					
MSE42	x					
MSE33	x					
MSE21	x					
MSE31	x					
MSE41	x					
MSE2	x					
MSE17	x	x				
MSE27	x	x				
MSE60	x	x				
MSE40	x	x				
MSE62	x	x				
MSE51	x	x	x			
MSE37	x	x	x			
MSE26	x	x	x			
MSE49	x	x	x			
MSE1		x				
MSE56		x				
MSE50				x	x	
MSE57			x			
MSE30	x	x	x			
MSE63		x	x	x		
MSE39		x	x	x	x	
MSE45	x	x	x	x	x	x
MSE13		x	x	x	x	x
MSE47		x	x	x	x	
MSE58		x	x	x		
MSE19		x	x			
MSE35		x	x			
MSE4		x	x			
MSE55	x					
MSE34	x					
MSE10			x	x		
MSE16			x	x		
MSE32			x	x		
MSE23			x	x	x	x
MSE46			x	x	x	x
MSE3			x	x	x	x
MSE36				x	x	x
MSE61				x	x	x
MSE20				x	x	x
MSE25				x	x	x

item	Y7	Y8	Y9	Y10	Y11	Y12
MSE53				x	x	x
MSE66				x		
MSE18				x		
MSE48					x	
MSE67					x	
MSE24					x	
MSE43					x	
MSE52					x	
MSE44					x	
MSE74					x	x
MSE75					x	x
MSE76				x	x	x
MSE69				x	x	x
MSE77						x
MSE78						x
MSE72						x
MSE68						x
MSE79						x
MSE70						x
MSE71						x
MSE73						x



## APPENDIX 4 – EXAMPLE OF MEASURE CONSTRUCTION FOR “PARENTAL INVOLVEMENT/SUPPORT”

As described above the starting ingredient in the process of measure construction is the questions. For the case of ‘parental involvement/support’, the items as appeared in the questionnaire (with some labels shown in red), are shown below:

How often do your parents/carers do the following?  
(Please circle the most appropriate number in each line)

	Never	Rarely	Sometimes	Often	All the time
Check whether you have done your homework [parents1]	1	2	3	4	5
Help you with your homework [parents2]	1	2	3	4	5
Praise or reward you for good grades [parents3]	1	2	3	4	5
Reduce your rewards because of low grades [parents4]	1	2	3	4	5
Find you a tutor to help you with your homework [parents5]	1	2	3	4	5

We hypothesise that these items form together an underlying construct of ‘students perception of parental involvement’ and we use the tools provided by the Rasch analysis to create and validate this measure (and others). Another necessary ingredient to perform this analysis/validation is the students’ responses to these questions which are denoted by the values 1 to 5, as shown above: the higher the score the more frequent each practice.

The ultimate outcome, if measurement is deemed valid, would be a score for each student on a logit scale, which can be used for further analysis. Our decisions about the validity of the measures are based on the following statistical indices, with the example results shown here:

### Item fit statistics

Fit statistics (i.e. Infit and Outfit mean-squares, MNSQ) are used in the Rasch context to check fulfilment of unidimensionality assumption and to flag items that may be problematic in this respect. In a ‘perfect’ measure these statistics should be 1, but an acceptable range is within 0.6 to 1.4 depending on the analysis. For most of our analyses we take the value of 1.4 as a value for infit and outfit mean squares that suggests causes for concern, and we explore those more.

ENTRY NUMBER	TOTAL SCORE	TOTAL COUNT	MEASURE	MODEL S.E.	INFIT		OUTFIT		PT-MEASURE		EXACT MATCH		ITEM
					MNSQ	ZSTD	MNSQ	ZSTD	CORR.	EXP.	OBS%	EXP%	
1	110814	30607	-.96	.01	.94	-7.4	.94	-7.6	.66	.63	40.8	39.7	parents1
2	89608	30548	-.20	.01	.72	-9.9	.76	-9.9	.66	.63	45.0	36.3	parents2
3	107576	30449	-.86	.01	1.00	-.4	1.00	-.4	.63	.63	39.1	39.7	parents3
4	64953	30388	.68	.01	1.16	9.9	1.19	9.9	.58	.61	38.9	39.1	parents4
5	51165	30429	1.34	.01	1.38	9.9	1.36	9.9	.53	.57	49.2	52.3	parents5
MEAN	84823.2	30484	.00	.01	1.04	.4	1.05	.4			42.6	41.4	
S.D.	23425.6	80.9	.89	.00	.22	8.3	.21	8.4			3.9	5.6	

Table A1 - Item statistics output from Winsteps

As shown in Table A1, there are no threats for this aspect of validity since all items appear within acceptable ranges.

## Category Statistics

Rating scales and their response formats serve as tools with which the researcher communicates with the respondents, a function defined by Lopez (1996) as ‘communication validity’. Examining category statistics is essential within the Rasch measurement framework in order to confirm the appropriateness of the Likert scale used and its interpretation by the respondents. A well-functioning scale should, at least, present ordered average measures, and ordered step calibrations (Linacre, 2002) with acceptable fit statistics, as shown here (see Table A2 and/or Figure A1). In the probability plot of Figure 2, the four thresholds (i.e. boundary between category 1 and 2, 2 and 3, 3 and 4, 4 and 5) are denoted with arrows superimposed on the probability curves of each category. Most of those seem to be ordered, however there is a small overlap between the first two boundaries, probably because of the ambiguity of response categories “rarely” and “sometimes”. An improved measure could be calculated by collapsing these two options (which also provides suggestions for improving the questionnaire).

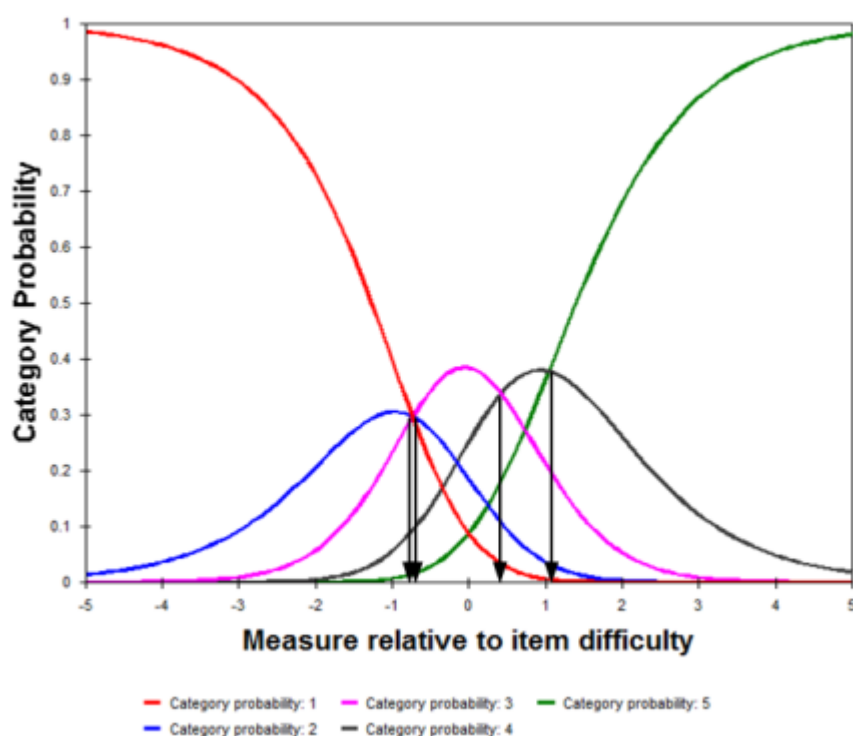


Figure A1 - Category probability against item difficulty

SUMMARY OF CATEGORY STRUCTURE. Model="R"

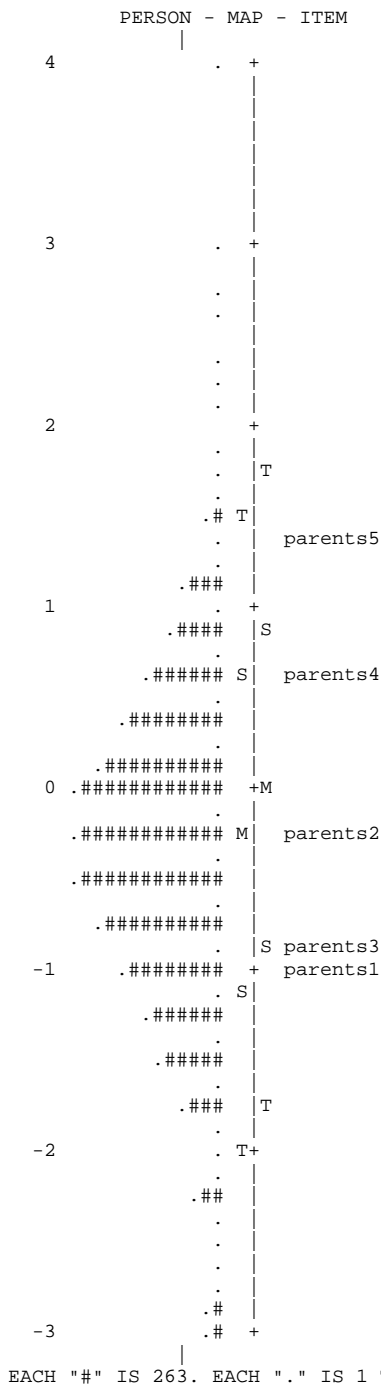
CATEGORY	OBSERVED	OBSVD	SAMPLE	INFIT	OUTFIT	STRUCTURE	CATEGORY			
LABEL	SCORE	COUNT	%	AVRGE	EXPECT	MNSQ	MNSQ	CALIBRATN	MEASURE	
1	1	41053	27	-1.57	-1.54	.93	.96	NONE	( -2.27)	1
2	2	25626	17	-.71	-.78	1.00	.94	-.74	-.97	2
3	3	34437	23	-.09	-.10	.94	.95	-.73	-.06	3
4	4	28025	18	.52	.51	1.01	1.13	.42	.93	4
5	5	23280	15	1.07	1.10	1.15	1.29	1.04	( 2.43)	5
MISSING		835	1	-.51						

OBSERVED AVERAGE is mean of measures in category. It is not a parameter estimate.

Table A2 - Category statistics output from Winsteps

## Person - item maps and the item difficulty hierarchy

Figure A2 shows the resulting measurement scale of students' scores and items' "difficulties". At the left end of the figure the logit scale is shown (with the numbers ranging from -3 to 4); this is the common measurement scale for both items and persons (i.e. students). On the right hand side of the students' 'histogram' the items that constitute the scale are presented, ranging from the easiest to report agreement with (bottom) to the most difficult. The description of the items that correspond to each code can be seen above. At the left side of the map the students' distribution in the scale is. The higher the place of a student in that scale the more parental support/involvement they perceive they receive.



**Figure A2** - Item map output from Winsteps

## APPENDIX 5 – SUMMARY OF ACCORN TYPES

Acorn Group		ACORN TYPE	Acorn Type 2
1. Affluent Achievers			
A	Lavish Lifestyles	1	Exclusive enclaves
		2	Metropolitan money
		3	Large house luxury
B	Executive Wealth	4	Asset rich families
		5	Wealthy countryside commuters
		6	Financially comfortable families
		7	Affluent professionals
		8	Prosperous suburban families
		9	Well-off edge of towners
C	Mature Money	10	Better-off villagers
		11	Settled suburbia, older people
		12	Retired and empty nesters
		13	Upmarket downsizers
2. Rising Prosperity			
D	City Sophisticates	14	Townhouse cosmopolitans
		15	Younger professionals in smaller flats
		16	Metropolitan professionals
		17	Socialising young renters
E	Career Climbers	18	Career driven young families
		19	First time buyers in small, modern homes
		20	Mixed metropolitan areas
3. Comfortable Communities			
F	Countryside Communities	21	Farms and cottages
		22	Larger families in rural areas
		23	Owner occupiers in small towns and villages
G	Successful Suburbs	24	Comfortably-off families in modern housing
		25	Larger family homes, multi-ethnic areas
		26	Semi-professional families, owner occupied neighbourhoods
H	Steady Neighbourhoods	27	Suburban semis, conventional attitudes
		28	Owner occupied terraces, average income
		29	Established suburbs, older families
I	Comfortable Seniors	30	Older people, neat and tidy neighbourhoods
		31	Elderly singles in purpose-built accommodation
J	Starting Out	32	Educated families in terraces, young children
		33	Smaller houses and starter homes

4. Financially Stretched			
K	Student Life	34	Student flats and halls of residence
		35	Term-time terraces
		36	Educated young people in flats and tenements
L	Modest Means	37	Low cost flats in suburban areas
		38	Semi-skilled workers in traditional neighbourhoods
		39	Fading owner occupied terraces
		40	High occupancy terraces, many Asian families
M	Striving Families	41	Labouring semi-rural estates
		42	Struggling young families in post-war terraces
		43	Families in right-to-buy estates
		44	Post-war estates, limited means
N	Poorer Pensioners	45	Pensioners in social housing, semis and terraces
		46	Elderly people in social rented flats
		47	Low income older people in smaller semis
		48	Pensioners and singles in social rented flats
5. Urban Adversity			
O	Young Hardship	49	Young families in low cost private flats
		50	Struggling younger people in mixed tenure
		51	Young people in small, low cost terraces
P	Struggling Estates	52	Poorer families, many children, terraced housing
		53	Low income terraces
		54	Multi-ethnic, purpose-built estates
		55	Deprived and ethnically diverse in flats
		56	Low income large families in social rented semis
Q	Difficult Circumstances	57	Social rented flats, families and single parents
		58	Singles and young families, some receiving benefits
		59	Deprived areas and high-rise flats
6. Not Private Households			
R	Not Private Households	60	Active communal population
		61	Inactive communal population
		62	Business addresses without resident population